

# **Mathematics**

# For First preparatory grade

first term

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غير مصرح بتداول هذا الكتاب خارج وزارة التربية والتعليم والتعليم الفني

#### Introduction

It gives us pleasure to introduce this book to our students of the first form preparatory, hoping that it will fulfill what we aimed for in regards of simplicity of the information included and clarity. We hope it helps train our generations to be able to think scientifically and be innovative.

The aspirations of the human have exceeded the limits of Earth and reached out into Outer Space. Every day and night, satellites and information networks report on current events from all over the world.

Due to technological progress, learning sources have become plentiful and various, and learning medias have also become numerous and more various than before. This has also caused teaching aids to become more complex, valuable and of greater impact.

#### While composing this book, the following was taken into consideration:

- Since studying number has not been enough for solving various life problems, so we must start studying mathematics that uses symbols instead of numbers to solve such problems.
- The use of images, shapes and colors to clarify mathematical concepts and properties of shapes.
- Integrating and linking between mathematics and other subjects.
- Designing educational situations that facilitate the use of active learning strategies and problem - solving skills.
- Display lessons in a way that allows students to deduce and construe information on their own.
- The book includes real-life issues, educational activities and situations related to problems environment, health, population issues in addition to the development of values such as human rights, equality, justice and developing concepts of Patriotism.
- Giving a variety of evaluation exercises at the end of each lesson, a test at the end of each
  unit and examinations at the end of the book.
- Include Activity models to implement the Overall (Comprehensive) Educational Assessment
- Employ technological methods.

#### This book has included four units:

Unit 1: Numbers - It aims at presenting the characteristics of numbers, representation of computational processes and understanding the relationships between them.

Unit 2: Algebra - It presents the meaning of algebraic terms and expressions and operations on them.

Unit 3: Geometry and measurement - it focuses on drawing 2 and 3 dimensional (shapes and solids) and being able to identify their properties and analyze the relations between them.

Unit 4: statistics - It alms at acknowledging data collection, organization and presentation as a way of finding a response to certain queries and passing judgement on interpretations and predictions based on the analysis of certain data.

While explaining the topics included in this book, it was taken into consideration that it must be as simple as possible with a wide variety of exercises to provide the students with the opportunity to think and create.

The Author

# List of symbols

There is a meaning for each mathematical symbol

Symbol	How read		
X = {,}	X is the set whose elements are		
Ø or { }	empty set or null set		
€	is an element of or belongs to		
<b></b>	is not an element of or does not belong to		
C	is a subset of or is contained in		
<b>⊄</b>	is not a subset of or is not contained in		
$X \cap Y = \{ a : a \in X \text{ and } a \in Y \}$	Intersection of two sets X and Y is the set which contains all the elements belonging to X and Y.		
$X \cup Y = \{ a : a \in X \text{ or } a \in Y \}$	Union of two sets X and Y is that set which contains all the elements belonging to X or Y.		
N	Set of Natural numbers { 0, 1, 2,}		
Z	Integers {, -2, -1, 0, 1, 2,}		
Z*	Set of positive integers { 1, 2, 3,}		
Z	Set of negative Integers { -1, -2, -3,}		
<b>≤</b>	is less than or equal to		
2	is greater than or equal to		

Symbol	How read		
pž.	is not equal to		
[a]	absolute value of a		
(a,b)	the ordered pair with first coordinate a and second coordinate b.		
$a \times a \times$ to n factors = $a^n$	the n <sup>th</sup> power for the number a		
√a	the square root of a		
//	is parallel to		
4	îs perpendicular to		
Δ	triangle		
*	Since		
i.	Therefore		
	right angle		
AB	Line segment AB		
AB	ray AB		
AB	Straight line AB		
_	Angle		
700	is congruent to		

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#### Unit 1

# Set of rational numbers

#### Muhamed Ibn Ahmed Abo Al Rihany Al Bairony

(363 H - 973 AD)

Al Bairony is one of the famous Arab Mathematicians. He stated that letters and digits vary in India by local variation and the Arabs took the best of what they have, then they refined some of them and formed two series known as:

\* Indian numbers

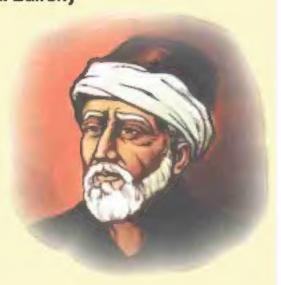
1, 1, 7, 2, 4, 1, 4, 4, 5, 5, 5

and are used by Eastern Arab.

Andalusian numbers (El Ghobaria):

9,8,7,6,5,4,3,2,1,0

and are used in Al Maghreb and Andalus.



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Mental Math.

Miscellaneous Exercises

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## Set of rational numbers

We know that

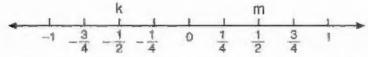
A rational number is a number that can be expressed in the form  $\frac{a}{b}$ , where a and b are integers and b  $\neq$  0.

The set of rational numbers  $Q = \{x: x = \frac{a}{b}, a, b \subseteq Z, b \neq 0\}$ 

 $Z \cap Q$ The set of Integers Z is a subset of the set of the rational numbers  $Q \rightarrow Z$  is a subset of Q



The set of rational numbers can be represented on the number line.



The point m is mid way between 0 and 1 represents the rational number  $\frac{1}{2}$ , and is read as positive half

The point k is mid way between 0 and -1 represents  $-\frac{1}{2}$  and is read as "negative half"

## Example (1)

Write the following numbers on the form a

[a] 
$$|-9\frac{1}{3}|$$
.

Solution:

[a] 
$$|-9\frac{1}{3}| = 9\frac{1}{3} = \frac{28}{3}$$

[b] 
$$0.15 = \frac{15}{100} = \frac{3}{20}$$

[c] 
$$40\% = \frac{40}{100} = \frac{4}{10} = \frac{2}{5}$$

#### Example (2)

Write the following numbers on the decimal and percentage form.

[a] 
$$\frac{16}{25}$$
.

[c] 
$$\frac{25}{8}$$
.

Solution:

[a] 
$$\frac{16}{25} = \frac{16 \times 4}{25 \times 4} = \frac{64}{100} = 0.64 = 64\%.$$

[b] 
$$|-2\frac{1}{4}| = \frac{9}{4} = 2.25 = 225\%$$
.

[c] 
$$\frac{25}{8} = 3 \cdot \frac{1}{8} = 3.125 = 312.5\%$$
.

#### Different forms of a rational number

Rational numbers such as <sup>3</sup>/<sub>4</sub> and <sup>7</sup>/<sub>5</sub> can be written as terminating decimals.

$$\frac{3}{4}$$
 = 0.75 = 0, 750 = ...

$$\frac{3}{4} = 0.75 = 0.750 = \dots$$
  $\frac{7}{5} = \frac{14}{10} = 1.4 = 1.40 = \dots$ 

• Rational numbers such as  $\frac{3}{4}$  and  $\frac{7}{5}$  can be written as

$$\frac{3}{4} = \frac{3 \times 25}{4 \times 25} = \frac{75}{100} = 75\%$$
  $\frac{7}{5} = \frac{7 \times 20}{5 \times 20} = \frac{140}{100} = 140\%$ 

$$\frac{7}{5} = \frac{7 \times 20}{5 \times 20} = \frac{140}{100} = 140\%$$

 Rational numbers such as <sup>1</sup>/<sub>3</sub> and <sup>2</sup>/<sub>11</sub> can be represented by an infinite repeating decimal.



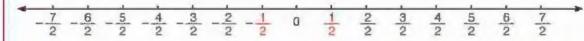
$$\frac{1}{3}$$
 = 0.333 ... = 0.3

$$\frac{2}{11} = 0.1818 \dots = 0.18$$

The point above the digit means that it is a repeating digit

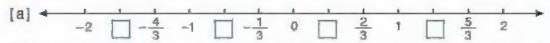
#### Exercise (1-1)

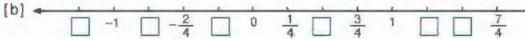
Use the number line to identify the opposite of each rational number in the table



Rational number	1 2	3 2	4/2	$-\frac{5}{2}$	7 2	$-\frac{3}{2}$	$-\frac{7}{2}$	2 2	- <del>6</del> 2	6 2
Opposite	-12									

Complete the rational numbers on the number lines.

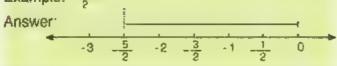






Use an arrow to represent each of the following numbers on the number line.

Example: - 5



- $[a] \frac{1}{2}$
- [b]  $-\frac{1}{3}$  [c]  $-\frac{4}{5}$
- [d]  $-3\frac{1}{2}$  [e]  $1\frac{1}{5}$



Classify each statement as true, T, or false, F. when a statement is false, tell why it is false.

[a]  $\frac{1}{3}$  is a natural number.

 $[b] - \frac{1}{3}$  is an integer.

[c]  $12\frac{5}{6}$  is a rational number.

[d] 6.5 is a rational number.

[e] The number 0 is neither positive nor negative.

[ f ] The number 0 is a counting number.



- [a] Why does the definition of a rational number  $\frac{a}{b}$  state that  $b \neq 0$ ?
  - [b] which rational number  $\frac{7}{11}$  or  $\frac{7}{20}$ , can be written as a terminating decimal?
  - [c] write a decimal for each rational number: 1)  $\frac{6}{11}$  2)  $-3\frac{1}{15}$
- [d] Evaluate:  $\left|-3\frac{1}{2}\right|$ ,  $\left|\frac{5}{8}\right|$ ,  $\left|-0.37\right|$ ,  $\left|-0.2\right|$ ,  $\left|-\frac{1}{3}\right|$

Write the following numbers in the form  $\frac{a}{b}$ :

- [a] 0.4
- [c] 30% [e] 8 2
- [6] 0.75
- dl zero
- If1-0.01

Write the following rational numbers as a decimal and a percentage.

- (b) 2 1
- $[c]7\frac{3}{16}$

 $[a] \frac{1}{6}$ 

 $[d] - \frac{3}{20}$ 

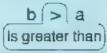
Lesson 2

## Comparing and ordering Rational numbers

The number line

On a number line, if the point representing a rational number "a" lies to the left of that representing "b", then

or



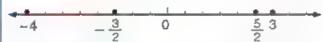
The ascending order of the rational numbers -3.0,  $2.-\frac{1}{2}$  is  $-3.-\frac{1}{2}$ , 0.2

The descending order of the rational numbers -3, 0, 2,  $-\frac{1}{2}$  is 2, 0,  $-\frac{1}{2}$ , -3

## Example 1

Represent the rational numbers 3,  $-\frac{3}{2}$ ,  $\frac{5}{2}$ , 0 and -4 on a number line, then rewrite them in an ascending order

Solution:



The order is  $1-4, -\frac{3}{2}, 0, \frac{5}{2}, 3$ 

#### Example 2

Which rational number is greater  $\frac{4}{7}$  or  $\frac{3}{5}$ ?

#### Solution:

The L.C.M. of 7 and 5 is 35

$$\frac{4}{7} = \frac{4 \times 5}{7 \times 5} = \frac{20}{35}$$
$$\frac{3}{5} = \frac{3 \times 7}{5 \times 7} = \frac{21}{35}$$

Since 21 > 20,  $\frac{21}{35}$  >  $\frac{20}{35}$  then  $\frac{3}{5}$  >  $\frac{4}{7}$ 

#### Example 3

Which rational number is greater  $-\frac{2}{3}$  or  $-\frac{3}{4}$ ?

#### Solution:

The L.C M. of 3 and 4 ls 12

$$-\frac{2}{3} = -\frac{2 \times 4}{3 \times 4} = \frac{8}{12}$$

$$-\frac{3}{4} = -\frac{3 \times 3}{4 \times 3} = -\frac{9}{12}$$
since  $-\frac{8}{12} > -\frac{9}{12}$ , then  $-\frac{2}{3} > -\frac{3}{4}$ 

## **Density of rational numbers**

#### Example 4

Find three rational numbers between  $\frac{4}{5}$  and  $\frac{2}{3}$ 

#### Solution:

The L.C.M. for the denominators 5 and 3 equals 15

$$\frac{4}{5} = \frac{4 \times 3}{5 \times 3} = \frac{12}{15}$$

$$\frac{2}{3} = \frac{2 \times 5}{3 \times 5} = \frac{10}{15}$$
The two rational numbers  $\frac{4}{5}$  and  $\frac{2}{3}$ 

because 
$$\frac{10}{15} < \frac{11}{15} < \frac{12}{15}$$

To find three rational numbers between them, multiply the numerator and denominator

of 
$$\frac{12}{15}$$
 and  $\frac{10}{15}$  by 2

$$\frac{12}{15} = \frac{12 \times 2}{15 \times 2} = \frac{24}{30}$$

$$\frac{10}{15} = \frac{10 \times 2}{15 \times 2} = \frac{20}{30}$$
The three required numbers are :  $\frac{21}{30}$ ,  $\frac{22}{30}$ ,  $\frac{23}{30}$ 

Because 
$$\frac{20}{30} < \frac{21}{30} < \frac{22}{30} < \frac{23}{30} < \frac{24}{30}$$

We can obtain an infinite number of rational numbers between  $\frac{4}{5}$  and  $\frac{2}{3}$ 

#### Deduction

Between any two different rational numbers there exists an infinite number of rational numbers, thus the rational numbers is dense

## Exercise (1-2)



[a] - 1 0

- [e] Every positive rational number
- [b] 3 14
- [f] Every negative rational number 0
- [c]-41 \_ -5
- [명]]-용[ ] 등
- [d] 4 1/2 5

 $[h] | \frac{15}{2} | \qquad 7 \frac{1}{2}$ 

Represent each set of the following rational numbers on the number line, and rewrite its elements in an ascending order.

 $[a] \{0, 1, -2, 3\}$ 

- [c] {2 \frac{1}{2}, \frac{1}{2}, -\frac{1}{4}, 1}
- [b]  $\{1, \frac{1}{2}, -2, \frac{1}{2}, 0, 2, \frac{1}{2}\}$
- $[d] \{-6.5, -4, -5, -3.5\}$

Which of the rational numbers is greater? Explain your answer.

[a] 4 or 3

 $[c] - \frac{7}{6}$  or  $-\frac{11}{15}$ 

[b]  $\frac{5}{8}$  or  $\frac{4}{8}$ 

 $[d] - \frac{8}{3}$  or  $-\frac{16}{7}$ 

Write the missing rational number.

- $[a] \frac{2}{5} < [c] \frac{1}{8} < [c] \frac{1}{4}$

- $[b] \frac{2}{3} < \Box < -\frac{1}{3}$   $[d] \frac{2}{7} < \Box < -\frac{3}{14}$

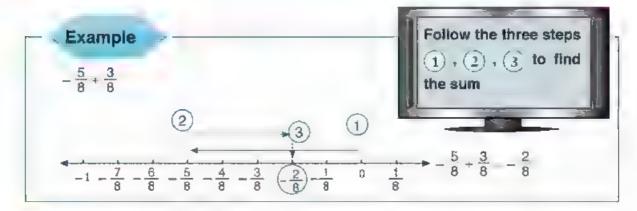
Write the rational number that equals  $\frac{3}{5}$ , and the sum of its terms is 24

- [a] Identify and write four rational numbers between  $\frac{3}{2}$  and  $\frac{3}{4}$ , such that one of them is an integer and the other is a rational number.
  - [b] Identify and write four rational numbers between  $\frac{-4}{9}$  and  $\frac{-5}{8}$

#### Lesson 3

## Addition of rational numbers

Represent the rational numbers on the number line will help you to add them.



## Complete

[8] 
$$\frac{3}{4} + () =$$

[b] 
$$\frac{1}{1}$$
  $\frac{1}{3}$   $\frac{2}{3}$   $\frac{1}{3}$   $\frac{4}{3}$   $\frac{5}{3}$   $\frac{2}{3}$   $\frac{1}{3}$   $\frac{4}{3}$   $\frac{5}{3}$   $\frac{2}{3}$ 

[c] 
$$\frac{1}{-\frac{7}{5}} \left( \frac{6}{5} \right)^{-1} - \frac{4}{5} - \frac{3}{5} - \frac{2}{5} - \frac{1}{5} = 0 \quad \frac{1}{5} \quad \frac{2}{5}$$
 ( )+( )= ...

Use the number line to add the following rational numbers:

a) 
$$\frac{5}{8} + (-\frac{3}{8})$$
 b)  $-\frac{1}{3} + \frac{5}{3}$ 

b) 
$$-\frac{1}{3} + \frac{5}{3}$$

c) 
$$-\frac{3}{4} + (-\frac{1}{4})$$

#### Example (2)

Find the value of each of the following in its simplest form:

$$[a] - \frac{4}{5} + (-\frac{3}{2})$$

[b] 
$$3\frac{1}{4} + (-2\frac{1}{3})$$

Solution:

[a] The L, C. M, of 5 and 2 is 10

$$-\frac{4}{5} + \left(-\frac{3}{2}\right) = -\frac{4 \times 2}{5 \times 2} + \left(-\frac{3 \times 5}{2 \times 5}\right)$$
$$= -\frac{8}{10} + \left(-\frac{15}{10}\right)$$
$$= -\frac{23}{10}$$

[b] The L. C. M. of 4 and 3 is 12

$$3\frac{1}{4} + (-2\frac{1}{3}) = 3\frac{1 \times 3}{4 \times 3} + (-2\frac{1 \times 4}{3 \times 4})$$
$$= 3\frac{3}{12} + (-2\frac{4}{12})$$
$$= 2\frac{15}{12} + (-2\frac{4}{12}) = \frac{11}{12}$$

### Example (3)

Find the value of each of the following in its simplest form:

[a] 
$$1 - \frac{5}{8} + (-7 - \frac{3}{4})$$

[b] 
$$\frac{1}{5} + (-4\frac{1}{3})$$

Solution:

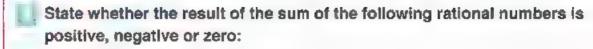
[a] The L.C.M of 8, 4 is 8

$$1\frac{5}{8} + (-7\frac{3}{4}) = 1\frac{5}{8} + (-7\frac{2\times3}{2\times4})$$
$$= 1\frac{5}{8} + (-7\frac{6}{8})$$
$$= -6\frac{1}{8}$$

[b] L.C.M of 5 and 3 is 15

$$\frac{1}{5} + \left(-4\frac{1}{3}\right) = \frac{3 \times 1}{3 \times 5} + \left(-4\frac{5 \times 1}{3 \times 5}\right)$$
$$= \frac{3}{15} + \left(-4\frac{5}{15}\right)$$
$$= -4\frac{2}{15}$$

#### Exercise (1-3)



$$[a] - \frac{3}{4} + (-\frac{1}{4})$$

[b] 
$$\frac{6}{7} + (-\frac{3}{7})$$

$$[c]\frac{12}{2} + (-\frac{16}{4})$$
  $[d]\frac{4}{3} + (-\frac{4}{3})$ 

$$[d]\frac{4}{3} + (-\frac{4}{3})$$

$$[e] - \frac{1}{5} + \frac{3}{5}$$

$$[e] - \frac{1}{5} + \frac{3}{5}$$
  $[f] - \frac{10}{100} + (-\frac{1}{10})$ 

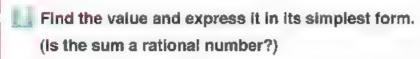
Find the value and express it in its simplest form:

$$[a] - \frac{3}{10} + (-\frac{2}{5})$$

[b] 
$$\frac{1}{4} + \frac{25}{8}$$

[c] 
$$\frac{19}{10} + (-\frac{39}{100})$$
 [d]  $-\frac{9}{12} + \frac{3}{16}$ 

$$[d] - \frac{9}{12} + \frac{3}{16}$$



[a] 
$$8\frac{2}{3} + (-5\frac{1}{6})$$
 [b]  $-15\frac{1}{2} + 2\frac{3}{8}$ 

[b] 
$$-15\frac{1}{2}+2\frac{3}{9}$$

[c] 
$$\frac{1}{4} + 2 \frac{3}{8}$$

$$[d] -8 \frac{1}{3} + (-4 \frac{1}{12})$$

[8] 
$$4 + (-9 \frac{5}{8})$$

$$[f] -2 + 13 - \frac{3}{7}$$

#### Lesson 4

# Properties of addition operation in the set of rational numbers

#### Complete

[a] 
$$\frac{2}{3} + \frac{3}{4} = \cdots$$

$$[b] \cdot \frac{3}{5} + \frac{2}{5} = \cdots$$

$$\frac{2}{5} + \left(-\frac{3}{5}\right) =$$

$$[c] \left(-\frac{5}{3} + \frac{2}{3}\right) + \frac{1}{3} = \left(-\right) + \frac{1}{3} = \cdots + \frac{5}{3} + \left(\frac{2}{3} + \frac{1}{3}\right) = -\frac{5}{3} + \cdots = \cdots$$

$$[d] - \frac{8}{3} + 0 = \cdots$$

$$0+(-\frac{4}{7})=....$$

[e] 
$$\frac{9}{8} + (-\frac{9}{8}) = \dots$$

Is the sum a rational number?

Are the sums equal in each case?

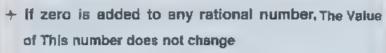
Does addition of rational numbers have the grouping property?

Does the value of a rational number change if you add to it zero?

What do you notice?

For every rational numbers  $\frac{a}{b}$ ,  $\frac{c}{d}$  and  $\frac{a}{l}$  then:

The property	The property Description in symbols	
1- Closure	$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd} \in Q$	If $\frac{1}{2}$ , $2 \in \mathbb{Q}$ then $\frac{1}{2} + 2 = \dots \in \mathbb{Q}$
2 - Commutative	$\frac{a}{b} + \frac{c}{d} = \frac{c}{d} + \frac{a}{b}$	
3 - Associative		
4 - Additive-identity	$\frac{a}{b} + 0 = 0 + \frac{a}{b} = \frac{a}{b}$	
5 - Addıtive-Inverse	For every $\frac{a}{b}$ , there exists the additive inverse $-\frac{a}{b}$ Where $\frac{a}{b} + (-\frac{a}{b}) = 0$	



- + 0 is the additive-identity element in Q
- + The additive inverse of zero is itself, the number zero.

#### Example (1)

Find the value of each of the following, stating the property:

$$[a] \frac{5}{10} + (\frac{-7}{10}), \qquad (\frac{-7}{10}) + \frac{5}{10}$$

[b] 
$$(\frac{1}{8} + \frac{3}{8}) + \frac{2}{8}$$
,  $\frac{1}{8} + (\frac{3}{8} + \frac{2}{8})$ 

$$[c] \frac{4}{5} + (\frac{-4}{5})$$
 ,  $\frac{-5}{12} + \frac{5}{12}$ 

Solution:

$$[a] \frac{5}{10} + (\frac{-7}{10}) = \frac{-2}{10}$$

$$\left(\frac{-7}{10}\right) + \frac{5}{10} = \frac{-2}{10}$$

$$\frac{5}{10} + (\frac{-7}{10}) = (\frac{-7}{10}) + \frac{5}{10} + \frac{-2}{10}$$

Commutative property

$$[b](\frac{1}{8} + \frac{3}{8}) + \frac{2}{8} = \frac{4}{8} + \frac{2}{8} = \frac{6}{8} = \frac{3}{4}$$

$$\frac{1}{8} + (\frac{3}{8} + \frac{2}{8}) = \frac{1}{8} + \frac{5}{8} = \frac{6}{8} = \frac{3}{4}$$

$$\therefore \left( \frac{1}{8} + \frac{3}{8} \right) + \frac{2}{8} = \frac{1}{8} + \left( \frac{3}{8} + \frac{2}{8} \right) = \frac{3}{4}$$

Associative property

$$[c] - \frac{4}{5} + (\frac{-4}{5}) = \frac{4 \cdot 4}{5} = Zero$$

$$\frac{-5}{12} + \frac{5}{12} = \frac{-5+5}{12} = Zero$$

Additive inverse property

#### Exercise (1-4)



$$[a] \frac{7}{2} + \frac{9}{16} = \frac{9}{16} + \frac{7}{2}$$

[b] 
$$\left[\frac{2}{3} + \left(-\frac{1}{3}\right)\right] + \left(-\frac{1}{6}\right) = \frac{2}{3} + \left[-\frac{1}{3} + \left(-\frac{1}{6}\right)\right]$$

$$[c]\frac{3}{4} + (-\frac{3}{4}) = 0$$

$$[d] \frac{5}{8} + 0 = (\frac{5}{8})$$

Find the sum of each of the following:

$$[a]\frac{4}{7} + 0$$

[d] 
$$\frac{5}{6} + (-\frac{3}{6} + \frac{3}{6})$$

[b] 
$$0 + (-\frac{7}{10})$$

$$[c][\frac{1}{4} + (-\frac{1}{4})] + \frac{3}{4}$$

[e] 
$$\left[\frac{2}{9} + \left(-\frac{4}{9}\right)\right] + \left(-\frac{3}{9}\right)$$

Write the additive inverse of each of the following rational number:

$$[a] \frac{3}{7}$$

$$[b] - \frac{4}{9}$$

$$[d] - 6$$

#### Mental Math

Complete

[a] 
$$14\frac{1}{2} + (-11\frac{1}{2}) = \dots + [11\frac{1}{2} + (-11\frac{1}{2})]$$

[b] 
$$\frac{3}{32} + (-\frac{17}{32}) = [\frac{3}{32} + (-\frac{3}{32})] + \dots$$

Find the sum in simplest form by using the properties of addition operation in Q:

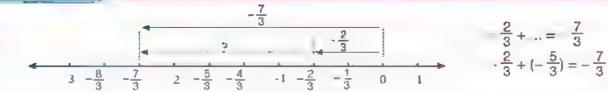
[a] 
$$7\frac{1}{4} + (-11\frac{1}{4})$$

[b] 
$$\frac{2}{3} + \frac{4}{5} + \frac{3}{4}$$

$$[c]-13\frac{1}{8}+7\frac{3}{8}$$

#### Lesson 5

## Subtraction of rational numbers



$$\frac{2}{3} + \dots = \frac{7}{3}$$
$$\cdot \frac{2}{3} + \left(-\frac{5}{3}\right) = -\frac{7}{3}$$

The subtraction operation  $(\frac{a}{b} - \frac{c}{d})$  is an addition operation of the minuend  $\frac{a}{b}$  with the additive inverse of the subtrahend  $\frac{c}{d}$ .  $\frac{a}{b} - \frac{c}{d} = \frac{a}{b} + \left(-\frac{c}{d}\right)$ 

#### Example

Calculate the value of each of the following in its simplest form:

$$[a] \frac{9}{2} - \frac{13}{4}$$

$$[b] - 3 \frac{2}{3} - 2 \frac{5}{8}$$

Solution:

[a] L.C.M. of 2 and 4 is 4

$$\frac{9}{2} - \frac{13}{4} = \frac{9 \times 2}{2 \times 2} + \left(-\frac{1}{4}\right)$$
$$= \frac{18}{4} + \left(-\frac{13}{4}\right)$$
$$= \frac{5}{4}$$

$$\frac{9}{2} - \frac{13}{4} = \frac{9 \times 2}{2 \times 2} + (-\frac{13}{4}) \qquad -3\frac{2}{3} - 2\frac{5}{6} = -3\frac{2 \times 2}{3 \times 2} + (-2\frac{5}{6})$$

$$= \frac{18}{4} + (-\frac{13}{4}) \qquad = -3\frac{4}{6} + (-2\frac{5}{6})$$

$$= \frac{6}{4} \qquad = -5\frac{9}{6} = -5\frac{3}{2} = -6\frac{1}{2}$$

#### Exercise (1-5)

Put ✓ for the correct statement and ☒ for the incorrect one:

$$\Box$$
 [c]  $0 - (-\frac{13}{5}) = \frac{13}{5}$ 

$$[b] - 3\frac{1}{6} - (-7\frac{1}{12}) = -3\frac{1}{6} + 7\frac{1}{12}$$
  $\Box$   $[d] - \frac{3}{4} - \frac{2}{5} = -\frac{3}{4} + \frac{2}{5}$ 

Calculate the value of each of the following in its simplest form:

[a] 
$$1\frac{3}{4} - (-2\frac{1}{2})$$
 [c]  $0 - (-\frac{17}{4})$  [e]  $-\frac{3}{5} - \frac{9}{5}$ 

$$[c]0-(-\frac{17}{4})$$

$$[e] - \frac{3}{5} - \frac{9}{5}$$

[b] 
$$-10\frac{7}{8} - (-4\frac{5}{8})$$
 [d]  $6\frac{2}{3} - 3\frac{1}{8}$  [f]  $-2\frac{1}{2} - 12\frac{1}{16}$ 

[d] 
$$6\frac{2}{3} - 3\frac{1}{6}$$

$$[f] - 2\frac{1}{2} - 12\frac{1}{16}$$

15

#### Lesson 6

# Multiplying of rational numbers

The product of two rational numbers

To multiply two rational numbers we must must ply their numerators to get the numerator of the product. Then multiply their denominators to get the denominator of the product.

$$\frac{2}{5} \times \frac{4}{3} = \frac{2 \times 4}{5 \times 3} = -$$

$$\frac{2}{5} \times \frac{4}{3} = \frac{2 \times 4}{5 \times 3} = \frac{2}{5} = \frac{2 \times 6}{3 \times 7} = \frac{2 \times 6}{3 \times 7}$$

If  $\frac{a}{b}$ ,  $\frac{c}{d}$  are two rational numbers, then  $\frac{a}{b} \times \frac{c}{d} = \frac{a \times c}{b \times d}$ If  $\frac{a}{b}$ ,  $\frac{c}{b}$  are two rational numbers, then  $\frac{a}{b} \times \frac{c}{b} = \frac{a \times c}{b^2}$ 

## Example (1)

Find the result of each of the following

$$[a] \frac{2}{5} \times \frac{4}{3}$$

[b] 
$$\frac{3}{7} \times \frac{-4}{5}$$

$$[c] \frac{-2}{9} \times \frac{-1}{9}$$

Solution:

$$[a] \frac{2}{5} \times \frac{4}{3} = \frac{2 \times 4}{5 \times 3} = \frac{8}{15}$$

[b] 
$$\frac{3}{7} \times \frac{-4}{5} = \frac{3 \times -4}{7 \times 5} = \frac{-12}{35}$$

[c] 
$$\frac{\cdot 2}{9} \times \frac{\cdot 1}{9} = \frac{\cdot 2 \times -1}{9 \times 9} = \frac{2}{9^2} = \frac{2}{81}$$

#### Exercise (1-6)

III Find the value of each of the following:

[a] 
$$\frac{3}{5} \times \frac{2}{7}$$

$$[d]-4\frac{2}{7}\times(-5\frac{1}{6})$$

$$[b] - \frac{3}{8} \times (\frac{-5}{3})$$

$$[e] - \frac{2}{3} \times \frac{5}{8}$$

[c] 
$$\frac{4}{5} \times (-\frac{3}{7})$$

[f] 
$$3\frac{1}{8} \times (-4\frac{1}{5})$$

Find the value of each of the following:

[a] 
$$1\frac{1}{2} \times \frac{4}{5}$$

$$[c] - \frac{5}{8} \times (-1 + \frac{1}{15})$$

[b] 
$$-\frac{3}{4} \times 1\frac{1}{9}$$

[d] 
$$2\frac{3}{7} \times \frac{7}{17}$$

Find the value of each of the following:

$$[a] \left| \frac{-3}{7} \right| \times \left( \frac{-4}{3} \right)$$

$$[c]2\frac{3}{4}\times(-3\frac{1}{5})$$

[b] 
$$-1 - \frac{1}{2} \times \frac{-5}{3}$$

$$[d]-4\frac{2}{7}\times(-8\frac{1}{6})$$

#### Lesson 7

# Properties of multiplication operation in the set of rational numbers



Multiply: 
$$\frac{2}{3} \times \frac{3}{4} = \cdots$$

is the product a rational number?

## Complete the table:

● x ▲		•	▲ × ●		
4 +**	1 2	3 5	maqdayd		
d wind winds	-47	-1/3	-		

Are the products equal if we change the position of the two numbers?

## Complete:

$$\frac{\left[-\frac{2}{5} \times \left(-\frac{3}{4}\right)\right] \times \frac{1}{3} = -\frac{2}{5} \times \left(-\frac{3}{4} \times \frac{1}{3}\right) = -\frac{2}{5} \times \left(-\frac{3}{4}\right) \times \frac{1}{3}}{\frac{20}{5} \times \frac{1}{3}} \qquad -\frac{2}{5} \times \frac{2}{12} \qquad \frac{-2 \times 2 \times 2}{5 \times 4 \times 3}}{\frac{20}{60}}$$

Does the multiplication of rational numbers have the grouping property?

[b] 
$$-\frac{3}{5} \times 1 = \cdots$$
,  $1 \times (-\frac{7}{8}) = \cdots$ .

Does the value of the rational number change if you multiply it by one?

[c] 
$$\frac{5}{9} \times \frac{9}{5} = \dots$$
,  $-\frac{7}{3} \times (-\frac{3}{7}) = \dots$  What do you notice?

[d] 
$$-\frac{1}{2} \times \left[\frac{3}{7} + \left(-\frac{2}{7}\right)\right] = -\frac{1}{2} \times \frac{\dots}{7} = \frac{\dots}{14}$$
  
 $-\frac{1}{2} \times \frac{3}{7} + \left(\left(-\frac{1}{2}\right) \times \frac{-2}{7}\right) = -\frac{\dots}{14} + \frac{\dots}{14} = \frac{\dots}{14}$ 

What do you notice?



For any three rational numbers  $\frac{a}{b}$ ,  $\frac{c}{d}$  and  $\frac{e}{t}$  then:

The property	Description in symbols	Example
1- Closure	$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd} \in Q$	If $-\frac{1}{4}$ , $-\frac{2}{3} \in \mathbb{Q}$ then $-\frac{1}{4} \times (-\frac{2}{3}) = \dots \in \mathbb{Q}$
2 - Commutative	$\frac{a}{b} \times \frac{c}{d} = \frac{c}{d} \times \frac{a}{b}$	
3 - Associative	$(\frac{a}{b} \times \frac{c}{d}) \times \frac{\theta}{f} = \frac{a}{b} \times (\frac{c}{d} \times \frac{\theta}{f})$ $= \frac{a}{b} \times \frac{c}{d} \times \frac{\theta}{f}$	
4 - Multiplicative-identity	$\frac{\mathbf{a}}{\mathbf{b}} \times 1 = 1 \times \frac{\mathbf{a}}{\mathbf{b}} = \frac{\mathbf{a}}{\mathbf{b}}$	
5 - Multiplicative-Inverse	For every rational number $\frac{a}{b} \neq 0$ , there exists a multiplicative inverse $\frac{b}{a}$ where: $\frac{a}{b} \times \frac{b}{a} = 1$	
6 - Multiplication distributes	$\frac{a}{b} \times (\frac{c}{d} + \frac{e}{f}) =$	
over addition	$\left(\frac{a}{b} \times \frac{c}{d}\right) + \left(\frac{a}{b} \times \frac{e}{f}\right)$	

- Multiplying a rational number by 1 does not change its value.
- Multiplying a rational number by zero, the product equals zero.
- + 1 is the multiplicative identity element in Q.
- There does not exist a multiplicative inverse for the number zero as <sup>1</sup>/<sub>0</sub> is meaningless.



#### Exercise (1-7)

State the property of the multiplication of rational numbers used in each of the following statements:

$$[a] - \frac{1}{2} \times \frac{2}{3} = \frac{2}{3} \times (-\frac{1}{2})$$

[d] 
$$\frac{5}{4} \times 1 = \frac{5}{4}$$

[b] 
$$-\frac{3}{7} \times (-\frac{7}{3}) = 1$$

[e] 
$$0.8 \times 0 = 0$$

$$[c] - \frac{7}{20} \times (\frac{5}{2} \times 4) = (\frac{5}{2} \times 4) (-\frac{7}{20})$$

Complete:

[a] 
$$\frac{2}{9} \times (-\frac{4}{5}) = -\frac{4}{5} \times ...$$

$$[d] - \frac{4}{11} \times \dots = 1$$

[b] 
$$\frac{2}{3}(2+\frac{1}{2})=\frac{2}{3}\times 2+ \dots$$

$$[c] \frac{2}{3} \times \frac{3}{2} = \dots$$

**Mental Math** 

Find the value of n in each of the following:

[a] 
$$\frac{5}{7} \times n = \frac{5}{7}$$

[d] 
$$n \times \frac{17}{3} = 1$$

$$[b] - \frac{7}{3} \times n = 0$$

$$[e] - \frac{7}{3} \times (-\frac{3}{7}) = n$$

$$[c] n \left[ \frac{1}{2} + \left( -\frac{3}{5} \right) \right] = n \times \frac{1}{2} + 5 \times \left( -\frac{3}{5} \right)$$

Use the properties of distribution of multiplication over addition of rational numbers to calculate each value:

[a] 
$$\frac{4}{9} \times 11 + \frac{4}{9} \times 16$$

$$[c] - \frac{3}{7} \times 6 + 5 \times (-\frac{3}{7}) + (-\frac{3}{7})$$

[b] 
$$\frac{5}{12} \times 3 + \frac{5}{12} \times 9$$

[d] 
$$\frac{18}{5} \times \frac{25}{9} + (-\frac{3}{7}) \times \frac{25}{9}$$

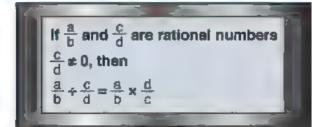
#### Division of two rational numbers

To divide the rational number  $-\frac{2}{3}$  by  $\frac{4}{5}$ 

You multiply  $-\frac{2}{3}$  by the multiplicative inverse of  $\frac{4}{5}$  which is  $\frac{5}{4}$ 

#### Complete:

$$-\frac{2}{3} \div \frac{4}{5} = -\frac{2}{3} \times \frac{5}{4} = -\frac{\cdots}{\cdots} = -\frac{\cdot}{\cdots}$$



#### Example (1)

#### Calculate the value of each of the following:

$$[a] - \frac{5}{4} \div (-\frac{2}{3})$$

$$[b] - 3\frac{3}{4} \div (-2\frac{1}{4})$$

#### Solution

Since the dividend and divisor are both negative, the quotient is positive

$$[a] - \frac{5}{4} + (-\frac{2}{3}) = -\frac{5}{4} \times (-\frac{3}{2})$$
$$= \frac{5 \times 3}{4 \times 2}$$
$$= \frac{15}{8}$$

$$[b] - 3\frac{3}{4} \div (-2\frac{1}{4})$$
$$\frac{15}{4} \div \frac{9}{4} = \frac{15}{4} \times \frac{4}{9}$$

$$=\frac{15}{9}=\frac{5}{3}$$

#### Example (2)

If  $a = \frac{3}{4}$ ,  $b = -\frac{5}{2}$ , find in simplest form the numerical value of:  $\frac{a - b}{a + b}$ 

#### Solution:

$$\frac{a-b}{a+b} = \frac{\frac{3}{4} - \left(-\frac{5}{2}\right)}{\frac{3}{4} + \left(-\frac{5}{2}\right)} = \frac{\frac{3}{4} + \left(\frac{5 \times 2}{2 \times 2}\right)}{\frac{3}{4} + \left(-\frac{5 \times 2}{2 \times 2}\right)} = \frac{\frac{3}{4} + \left(\frac{10}{4}\right)}{\frac{3}{4} + \left(-\frac{10}{4}\right)} = \frac{\frac{13}{4}}{-\frac{7}{4}}$$
$$= \frac{13}{4} \times \left(-\frac{4}{7}\right) = -\frac{13}{7}$$

#### Exercise (1-8)

Calculate the value of each of the following, then put the result in its simplest form:

[a] 
$$\frac{4}{5} \div \frac{3}{7}$$

[d] 
$$0 \div \frac{3}{5}$$

[b] 
$$\frac{8}{3} + (-\frac{15}{7})$$

$$[e] - \frac{4}{5} + \frac{7}{2}$$

$$[c] - 14 - (-\frac{4}{7})$$

$$[1] \frac{3}{8} \div (-7)$$

Calculate the value of each of the following, then put the result in its simplest form:

$$[a] - 2\frac{1}{5} \div 5\frac{1}{2}$$

$$[c]-4\frac{2}{7}\div(1\frac{1}{14})$$

[b] 
$$-2\frac{3}{4} \div (-3\frac{1}{8})$$

[d] 
$$6\frac{1}{4} \div (-15)$$

Calculate the value of each of the following, then put the result in Its simplest form:

$$[a](-\frac{18}{5} \div \frac{9}{35}) \times (-\frac{3}{7})$$
  $[c]-1+2\frac{1}{4}$ 

$$[c]-1+2\frac{1}{4}$$

[b] 
$$(-1\frac{2}{3} \times 4\frac{2}{3}) \div 6\frac{1}{9}$$

[b] 
$$(-1\frac{2}{3} \times 4\frac{2}{3}) \div 6\frac{1}{9}$$
 [d]  $[-\frac{12}{25} \times (-\frac{5}{7})] \div (-\frac{9}{14})$ 

If  $x = \frac{3}{2}$ ,  $y = -\frac{1}{4}$  and z = -2, find the simplest form of the numerical value of each of the following:

[a] 
$$(x + z) \div (y - z)$$

$$[b] \frac{x+y}{z}$$

#### Example (1)

Find the rational number half way between  $\frac{9}{4}$  and  $\frac{17}{6}$ 

#### Solution:

If the smaller number is  $\frac{9}{4}$  and the greater number is  $\frac{17}{8}$ ,

$$\frac{9}{4} + \frac{1}{2} \left( \frac{17}{6} - \frac{9}{4} \right) = \frac{9}{4} + \frac{1}{2} \left[ \frac{34}{12} + \left( -\frac{27}{12} \right) \right]$$

$$= \frac{9}{4} + \frac{1}{2} \times \frac{7}{12}$$

$$= \frac{9}{4} + \frac{7}{24} = \frac{54}{24} + \frac{7}{24} = \frac{61}{24} \qquad \text{L.C.M of 4, 24 is 24}$$

Then  $\frac{61}{24}$  is a rational number between  $\frac{9}{4}$  and  $\frac{17}{8}$ 

#### Example (2)

Find the rational number that lies one third of the way between  $-\frac{5}{6}$  and  $-1\frac{1}{2}$  from the smaller.

#### Solution:

If the smaller number is  $-1 \frac{1}{2} = -\frac{9}{6}$  and the greater number is  $-\frac{5}{6}$ .

$$-\frac{9}{6} + \frac{1}{3} \left[ -\frac{6}{6} - \left( \frac{-9}{6} \right) \right] = -\frac{9}{6} + \frac{1}{3} \times \frac{4}{6} = -\frac{9}{6} + \frac{4}{18} = -\frac{27}{18} + \frac{4}{18} = -\frac{23}{18}$$

Then  $-\frac{23}{18}$  is a rational number that lies one third from  $-1\frac{1}{2}$  to  $-\frac{5}{6}$ 

Is there a rational number that lies one third of the way from  $-\frac{5}{6}$  to  $-1\frac{1}{2}$ ? due to the smallest

#### Exercise (1-9)



[a] If 
$$a \times \frac{b}{2} = \frac{a}{2}$$
, then  $b = \dots$ 

[b] If 
$$\frac{x}{3} - 4 = 6$$
, then  $\frac{x}{3} + \frac{2}{3} = \dots$ 

$$[1, x, \frac{32}{3}, 10]$$

[c] If 
$$4x - y = 11$$
,  $y = 3x$ , then  $x = ....$ 

[d] If 
$$\frac{x}{y} = 1$$
, then  $2x - 2y = ....$ ,

Find the rational number in half-way between each of the following

$$[a] \frac{3}{8}, \frac{4}{9}$$

$$[d] - \frac{37}{180}, -\frac{9}{42}$$

[b] 
$$\frac{7}{11}$$
,  $\frac{3}{4}$ 

[e] 
$$-4\frac{3}{5}$$
,  $-5\frac{5}{6}$ 

$$[c] - \frac{11}{9}, -\frac{13}{35}$$

$$[f]-4\frac{3}{7}, 8\frac{1}{3}$$

[a] Find the rational number that lies one third of the way between  $\frac{4}{7}$  and  $1\frac{3}{4}$  from the smaller

- [b] Find the number one fourth of the way between  $-\frac{1}{9}$  and  $-\frac{7}{8}$  from the smallest,
- [c] Find the number one fifth of the way between  $-\frac{2}{3}$  and  $-\frac{3}{5}$  from the smaller.
- [d] Find a rational number between  $\frac{1}{3}$  and  $\frac{3}{4}$
- [e] Find a rational number between  $-\frac{1}{5}$  and  $-\frac{1}{9}$

#### Miscellaneous Exercises

# Mark ✓ for the correct statement and ✓ for the incorrect one:

[e] The rational numbers 
$$\frac{12}{16}$$
,  $\frac{15}{20}$  and  $\frac{3}{4}$  are represented with the same point on the number line

[f] 
$$2\frac{1}{5}$$
 is the multiplicative inverse for the rational number  $5\frac{1}{4}$ 

[g] 
$$\frac{3}{x-3}$$
 is the additive inverse for the rational number  $\frac{3}{3-x}$ , where  $x \ge 3$ 

[h] 
$$(\frac{2}{7} + \frac{3}{5})$$
 is the multiplicative inverse for the rational number  $\frac{35}{31}$ 

## Select the correct value:

[a] If 
$$x + \frac{2}{x} = 5 + \frac{2}{5}$$
, then  $x = ...$   $\left[\frac{1}{5}, \frac{4}{5}, \frac{5}{2}, 5\right]$ 

[b] If 
$$5a = 45$$
,  $ab = 1$ , then  $b = ...$   $\left[\frac{1}{45}, \frac{1}{9}, \frac{1}{5}, 9\right]$ 

[c] if 
$$\frac{x}{y} = \frac{2}{3}$$
, then  $\frac{3x}{2y} = \dots$  [ $\frac{1}{3}$ , 1,  $\frac{3}{2}$ ,  $\frac{9}{4}$ ]

[d] If 
$$3x = 42$$
, then  $\frac{5}{7}x = ...$  [70, 45, 30, 10]

## Complete in the same pattern:

[a] 6, 5 
$$\frac{1}{4}$$
,  $4\frac{1}{2}$ , ..., ...,  $\frac{3}{4}$ 

[b] 8, -4, 2, ..., 
$$\frac{1}{8}$$

# If $x = -\frac{1}{3}$ , $y = \frac{3}{4}$ , z = -3, find the numerical value of each of the following.

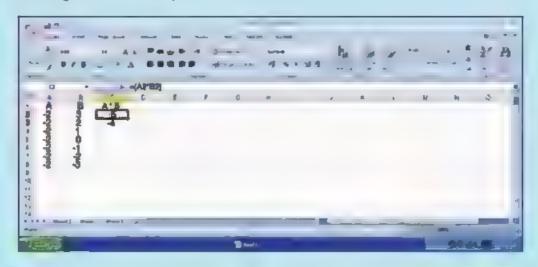
$$[c] \frac{xy}{z}$$

$$[b] \times y + y z$$

$$[d]\frac{x}{y} - \frac{y}{z}$$

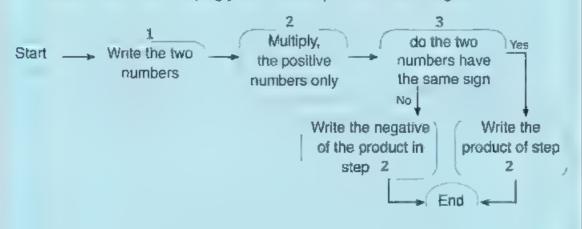
## Activity (1):

Use the spreadsheet "Excel" to find the product of two integers Click the start button on the task bar from the list of programs ... choose Microsoft Excel by copying and completing the table (Hint: Drag the "fill handle")



- [a] Extend your spreadsheet up to row 15 using other values of a and b.
- [b] Save what you have done in your folder

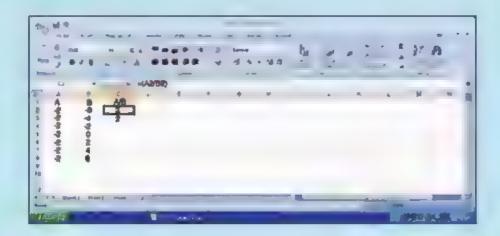
The flow chart below helping you to find the product of two integers.



## Activity (2):

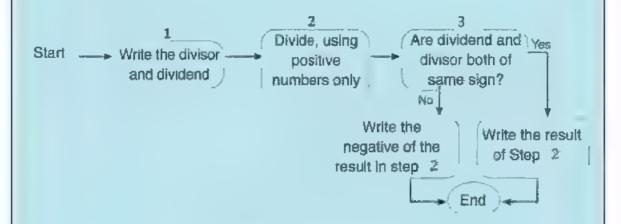
Use the spread sheet "Excel" to find the quotient of two integers by copying and completing the table

(Hint: Drag the "filt handle")



- [a] Extend your spreadsheet up to row 15 using other values of a and b.
  - [b] Save what you have done in your folder

The flow chart below suggests a means of computing the quotient of two integers.



#### **Unit test**



- (a) The multiplicative inverse of the rational number  $-\frac{2}{3}$  is ...
- [b] To find the quotient of dividing  $-\frac{7}{12}$  by  $-\frac{3}{2}$ , we have to multiply ...... by ......
- [c] 0 + (-14) = .....
- $[d] \frac{4}{3} \times (-\frac{3}{4}) = .$
- [e] The rational number half way between  $\frac{3}{5}$ ,  $\frac{4}{5}$  is ....
- $[f]\frac{2}{3} \times (2 + \frac{1}{2}) = \frac{2}{3} \times 2 + \frac{2}{3} \times \dots$

Write the rational number n which makes each of the statements true:

$$[a] - \frac{3}{5} \times - \frac{5}{3} = n$$

[b] 
$$(-3\frac{2}{3}) \times n = -3\frac{2}{3}$$

[c] The multiplicative inverse of  $1\frac{2}{3}$  is n

$$[d] n \times \left[\frac{3}{4} + \left(-\frac{2}{3}\right)\right] = \frac{1}{2} \times \frac{3}{4} + \frac{1}{2} \times \left(\frac{-2}{3}\right)$$

Evaluate:

$$[a] \frac{3}{4} \times (\frac{1}{2} - \frac{1}{3})$$

$$[d] \frac{3}{4} \times (\frac{1}{2} - \frac{1}{3})$$
 
$$[d] \frac{7}{12} \times \frac{23}{45} + \frac{17}{12} \times \frac{23}{45} - 2 \times \frac{23}{45}$$

[b] 
$$\frac{3}{5} \div (-\frac{9}{15})$$

$$\{e\}\left(\frac{1}{2} + \frac{3}{7}\right) \times \left[\frac{2}{6} + \left(-\frac{4}{5}\right)\right]$$

$$[c] - 3\frac{1}{2} \div (-2\frac{1}{4})$$

- [3] [a] If water flows through a pipe at the rate of  $2\frac{1}{2}$  litres per minute, how many minutes will it take to fill three 20 litre containers?
  - [b] How many pieces of wire  $3\frac{3}{4}$  metres long can be cut from a wire 60 metres long? Will any wire be left over? If so, how much?



→ Put the suitable sign (<, =, >):

$$[a] - 3\frac{1}{2} \square - 4$$

$$[d] \left| -\frac{13}{2} \right| \qquad 6\frac{1}{2}$$

[e] 
$$\frac{392}{9}$$
  $\square$   $44\frac{5}{8}$ 

$$[c] - \frac{7}{3} \square 0$$

[f] 
$$-\frac{214}{14}$$
  $-15\frac{2}{3}$ 

[a] If  $x = \frac{3}{2}$ ,  $y = -\frac{1}{4}$  and z = -2, Find in simplest form the numerical value of each of the following

(1) 
$$x - z + y$$
 (2)  $\frac{x}{y} - \frac{z}{y}$  (3)  $\frac{1}{xyz}$ 

$$(2) \frac{x}{y} - \frac{z}{y}$$

(3) 
$$\frac{1}{xyz}$$

[b] Find the product of:

$$\frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \frac{4}{5} \times ... \times \frac{99}{100}$$

What is the product when the last rational number is  $\frac{n-1}{n}$ ?

# Unit 2 Algebra

#### Muhamed Ibn Moussa Al Khowarezmy

(771 - 849)

Muslim, and Iraqi scientist

Arab are the first to use the word Algebra, the first of them is Al khowarezmy (the father of Algebra), thanks to Al khowarezmy, the world knew the use of the Arab digits which changed our concept of numbers, he also introduced the concept of zero.



#### Contents

Lesson 1 : Algebraic terms and Algebraic expressions

Lesson 2 : like terms.

Lesson 3: Multiplying and dividing Algebraic terms.

Lesson 4: Adding and subtracting Algebraic expressions.

Lesson 5: Multiplying a monomial by an Algebraic expression.

Lesson 6 : Multiplying a binomial by an Algebraic expression.

Lesson 7 Dividing an Algebraic expression by a monomial.

Lesson 8: Factorization by taking out the H.C.F.

Miscellaneous Exercises

Activities unit

Unit test.

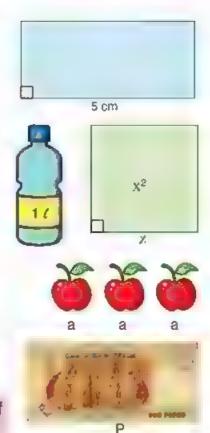
### Lesson 1

# Algebraic terms and Algebraic expressions

Mathematics is the language of symbols, We use the different symbols to express things or numbers, and we use these symbols by methods similar to that we use with numbers, for example:

- The length of this rectangle is 5 cm.
- The capacity of the bottle is "!" litres.
- If the letter x stands for the length of the side of a square then x x x = x² stands for its area.
- If the letter "a" stands for 1 apple, then
   a + a + a = 3 x a = 3 a stands for 3 apples and is
   called an algebraic term (monomial).
- If the letter P stands for 1 pound, then -2P stands for losing 2 pounds;

 $(-P) + (-P) = -2 \times P = -2P$ , and is called an algebraic term (monomial).



The algebraic term is formed from the product of two or more factors.

The algebraic term  $a = 1 \times a$  consists of 2 factors. 1 (numerical), and a (algebraic).

The algebraic term  $7x^2 = 7x \times x \times x$  consists of 3 factors:

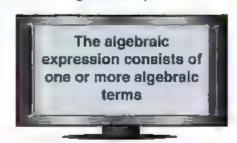
7 (numerical), x (algebraic), and x (algebraic).

The algebraic term 3a is of first degree because the index of a is 1

The algebraic term  $7x^2$  is of second degree because the index of x is 2

If we add the two terms 3a and  $7x^2$ , then  $3a + 7x^2$  is called an algebraic expression. If we subtract 2P from  $3a + 7x^2$ , then  $3a + 7x^2 - 2P$  is an called algebraic expression.

The algebraic expression  $4x^3 - xy + 5$  is of the third degree because The index of x is the highest degree of the terms forming it.



### Exercise (2-1)

### Complete:

Algebraic term	Coefficient	Degree	
<b>—</b> 7	<del>-</del> 7	0	
2ab²	2	1 + 2 = 3	
3	*100 1100	19 1407 1	
7ab³ c	*** * ***	*** **	
−8x² b			
x y²	из шь	103111051	

### Complete:

Algebraic express.on	Number of terms	Name	Degree
−3a⁵ b	1	Monomial	6
3x <sup>2</sup> + y	2	binomial	2
$5x^3 - 7x + 4$		trinomial	
2a² b + 3ab² - a² b²			
$x^2 y^2 - 3xy^4$			
$a^2 b - 3 ab^3 + 2a^3 b^2 + b^4$			

- [a] Arrange the terms of the algebraic expression 7ab + 5a<sup>5</sup> b<sup>3</sup> 3a<sup>2</sup> b<sup>5</sup> according to the descending order of the indices of a.
  - [b] Arrange the terms of the algebraic expression  $5x + x^2 7 + x^3$  according to the ascending order of the indices of x.

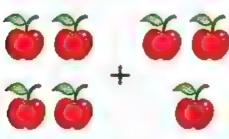
# In this figure:

Write the algebraic expression which represents the area of the shaded region then state its degree.

area of circle = m r2

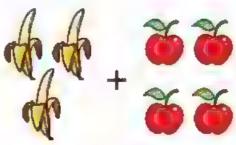
### Lesson 2 Like terms

Algebraic terms are similar if the symbols forming its factors are similar and the indices of these symbols are similar.



4a + 3a = 7a

The terms 3a and 4a are like terms.



3b + 4a

The terms 3b and 4a are unlike terms.

In adding and subtracting like terms, we add and subtract the coefficients of the terms, but the algebraic factors remain as they are.

### Example (1)

Simplify: 9a - 4b - 2c - 5a + 7b + 3c

Solution:

The expression = 
$$(9a - 5a) + (-4b + 7b) + (-2c + 3c)$$
  
=  $(9 - 5) a + (-4 + 7) b + (-2 + 3) c$   
=  $4a + 3b + c$ 

the expression contains groups of like terms so we use commutative, and distributive properties because unlike terms can not be added

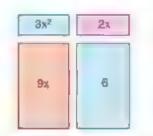
### Example (2)

### In this figure:

Write the expression which represents areas of the rectangles.

### Solution:

The sum of areas =  $3x^2 + 2x + 9x + 6$ =  $3x^2 + (2 + 9)x + 6$ =  $3x^2 + 11x + 6$ 



### Exercise (2-2)

Complete:

Algebraic terms	Like terms	Unlike terms
-2 x , 2 x y , x , - y	-2x,x	
~ ab <sup>2</sup> , 2a <sup>2</sup> b , 3b <sup>2</sup> a , ~ ab		2a² b , – ab
x2 y2, x2, y2, -3 x2 y2		
$3 a^4, -4 a^3, a^2, -3 a^2$		

Simplify:

[a] 
$$3x - 5y - x + 2y$$

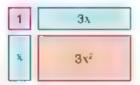
[c] 
$$2x - 4y - 9x - 3y$$

$$[b] 7a + 6b - 11a + 9b$$

$$[d] 19m - 4n + 11m - 17n + 9n$$

Write down the algebraic expressions which represent the sum of the areas of the follwing rectangles:

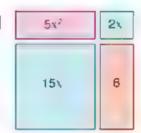
[a]



[b]



[C]



Simplify:

[a] 
$$5x - 3x^2 + 4 - 7x^2 - 6x - 1$$

[b] 
$$6x^2y - 3xy^2 + 2xy^2 - 5x^2y + 2x^2y^2$$

$$[c] a^2 + 4a - 5 + 3a^2 - 6a + 1$$

[d] 
$$5x^2 - 2x + 8 - 7x - 3 + x^2$$

# Lesson 3 Multiplying and dividing algebraic terms

When multiplying the term 5a by the term 3b, we write:

$$5a \times 3b = 5 \times a \times 3 \times b$$
  
=  $(5 \times 3) \times (a \times b)$   
= 15 ab

i.e we multiply the coefficients and then the symbols.

When multiplying 5x2 by 3x3, we write:

	b	ь	b
a	ab		
a			
a			
a			
a			

$$5x^2 \times 3x^3 = (5 \times 3) \times (x^2 \times x^3)$$
 What happens when multiplying the like bases? = 15x

When multiplying, we add the indices if the bases are equal.
When dividing, we subtract the indices if the bases are equal.

### Complete:

[a] 
$$X^2 \times X^3 = (X \times X) \times (X \times X \times X)$$
  
=  $X^+ = X$ 

[b] 
$$-2x^8 \times (-5x^2) = (-2 \times -5) \times x^8 \times x^2$$
  
= 10x

[c] 
$$\frac{x^{5}}{x^{3}} = \frac{x \times x \times x \times x \times x}{x \times x \times x}$$
$$= x = x$$
[d] 
$$\frac{2 \times x^{6}}{x^{5}} = \frac{2}{x^{5}} \times x$$

## Example (1)

Multiply each of the following

[a] 
$$\frac{1}{2}$$
 y<sup>4</sup> × 2y<sup>2</sup>

[c] - 3b<sup>8</sup> × 
$$\frac{1}{6}$$
 b

[b] 
$$\frac{21}{4}$$
  $x^5 \times \frac{2}{7}$   $x^8$ 

Solution:

[a] 
$$\frac{1}{2}$$
 y<sup>4</sup> x 2y<sup>2</sup> = y<sup>4+2</sup> = y<sup>6</sup>

[b] 
$$\frac{21}{4} x^5 \times \frac{2}{7} x^9 = \frac{3}{2} x^{5+3} = \frac{3}{2} x^8$$

[c] 
$$-3b^6 \times \frac{1}{6}b = \frac{-3}{6}b^{6+1} = \frac{-1}{2}b^7$$

### Example (2)

The length of a rectangle is 4x cm and its width is 3x cm, calculate its area.



### Solution:

area of the rectangle = length x width

$$= 4x \times 3x = 12x^2 \text{ cm}^2$$

### Example (3)

Divide each of the following

[a] 
$$\frac{4 \text{ a } b^3}{8 \text{ a b}}$$
 [b]  $\frac{3 \text{ m}^2 \text{ n}^4}{27 \text{ m } n^2}$ 

(b) 
$$\frac{3 \text{ m}^2 \text{ n}^4}{27 \text{ m n}^2}$$

Solution:

[a] 
$$\frac{4 \text{ a b}^8}{8 \text{ a b}} = \frac{1}{2} \text{ xa}^{1-1} \text{ x b}^{3-1} = \frac{1}{2} \text{ a}^0 \text{ b}^2 = \frac{1}{2} \text{ b}^2$$

[b] 
$$\frac{3 \text{ m}^2 \text{ n}^4}{27 \text{ m n}^2} = \frac{1}{9} \text{ m}^{2-1} \times \text{n}^{4-2} = \frac{1}{9} \times \text{m} \times \text{n}^2 = \frac{1}{9} \text{ m} \text{n}^2$$

### Example (4)

Three tennis balls fit into a box. Calculate the ratio between the volume of the three balls and the volume of the box?

### Solution:

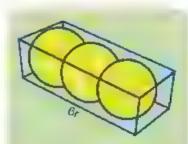
Let "r" be the radius of the ball, The dimensions of the box, 6r, 2r, 2r

Ratio of the space occupied by the balls to the volume.

of the box is Volume of 3 balls Volume of the box

$$= \frac{3 \times \frac{4}{3} \pi r^3}{6 \Gamma \times 2 \Gamma \times 2 \Gamma} = \frac{4 \pi r^3}{24 r^3} = \frac{\pi}{6}$$

- 0.52 The three balls occupy over half the space of the box



Volume of sphere = 
$$\frac{4}{3} \pi r^3$$
  
 $\pi = 3.14$ 

### Exercise (2-3)

## Multiply or divide:

$$[c] - 8 y^5 \times (-7 y^4)$$

[d] 
$$9 x^8 y^4 \div 6 x^3 y$$

$$[f] - 32 a^3 b^6 \div (-4 a^3 b^2)$$

### 🗾 Multiply:

[a] 
$$\frac{2}{3}t^4 \times \frac{3}{2}t^4$$

[b] 
$$\frac{2}{7}$$
  $a^2 \times 21$   $a^8$ 

[c] 
$$\frac{15 a^3 b}{2} \times \frac{8 ab^2}{10}$$

[d] 
$$3x^3 \times \frac{1}{6}x^2$$

[e] 
$$\frac{4 h^3 k^3}{7} \times \frac{21 h k^5}{2}$$

[f] 
$$4m^3 \times \frac{1}{4} m^2 \times (-7m)$$

### Complete:

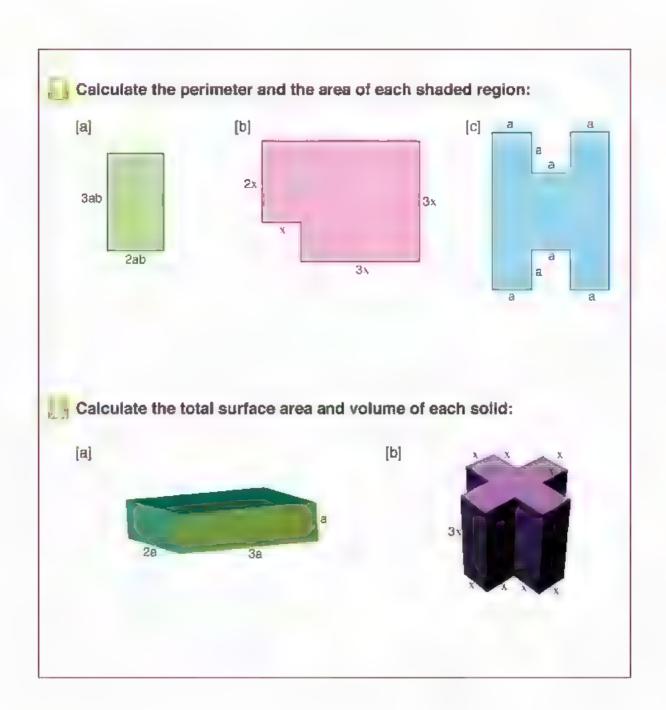
[a] 
$$36 a^5 b^8 = 12 a^3 b^2 x ----$$

[6] 
$$-4c^3d^3 = 2 ed^2 \times \cdots$$

[d] 
$$98a^7 b^4 = \cdots \times 14 a^7 b$$

[e] 
$$36a^8b^5 = 6ab^2 \times 3a^4b \times$$

[#] 
$$42x^4y^5 = 3x^2y \times 2xy \times \cdots$$



# Lesson 4 Adding and subtracting algebraic expressions

Adding and subtracting algebraic expressions does not differ from adding and subtracting algebraic terms. That is by adding like terms in the expressions each one alone, or subtracting like terms in the expressions each one alone.

### Example (1)

Add 2X - 5z + y and 7X + 4y - 2z

### Solution

Using the horizontal method

The sum = 
$$2x - 5z + y + 7x + 4y - 2z$$
  
=  $(2x + 7x) + (-5z - 2z) + (y + 4y)$   
=  $9x - 7z + 5y$ 

Using the vertical method

$$2x - 5z + y$$

$$7x - 2z + 4y$$

The sum = 
$$9x - 7z + 5y$$

### Example (2)

Subtract  $-a^2 - 5ab + 4b^2$  from  $3a^2 - 2ab - 2b^2$ 

### Solution:

### Using the horizontal method

The remainder = 
$$3a^2 - 2ab - 2b^2 - (-a^2 - 5ab + 4b^2)$$
  
=  $3a^2 - 2ab - 2b^2 + a^2 + 5ab - 4b^2$   
=  $(3a^2 + a^2) + (-2ab + 5ab) + (-2b^2 - 4b^2)$   
=  $4a^2 + 3ab - 6b^2$ 

### Using the vertical method

### Change the signs of the second expression then add

$$3a^2 - 2ab - 2b^2$$

The remainder =  $4a^2 + 3ab - 6b^2$ 

### Exercise (2-4)



[a] 
$$(3x - 2y + 5)$$
 and  $(x + 2y - 2)$ 

[a] 
$$(3x - 2y + 5)$$
 and  $(x + 2y - 2)$  [c]  $(3x^2 - 4x - 2)$  and  $(-x^2 - 4x + 7)$ 

[b] 
$$(3n^2 + 5n - 6)$$
 and  $(-n^2 - 3n + 3)$  [d]  $(3a^3 - 2ab^2)$  and  $(a^3 - 4ab^2 - b^3)$ 

[d] 
$$(3a^3 - 2ab^2)$$
 and  $(a^3 - 4ab^2 - b^3)$ 

Find the sum of each of the following expressions:

[a] 
$$3x - 4y + 2$$
  
 $-3x + 7y + 3$ 

[b] 
$$3a-7b-5c+2$$
  
-a +4b+c -5

[b] 
$$3a-7b-5c+2$$
 [c]  $5x+2y-z+2$ 

$$7x + y - 3z + 3$$

$$2a + 3c + 3 - 2x - 5y + 4z - 1$$

Subtract:

[a] 
$$(x-2)$$
 from  $(2x-5)$ 

[b] 
$$(2x + 6y - 7)$$
 from  $(2x - 5y + 2)$ 

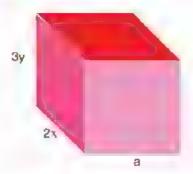
[c] 
$$(a+2b+3)$$
 from  $(a-3b+5)$ 

[d] 
$$(-x^2 - 4x + 7)$$
 from  $(3x^2 - 4x - 2)$ 

[a] What is the increase of  $x^2 - 5x - 1$  than  $3x^2 + 2x - 3$ 

[b] What is the decrease of 2x - 8y - z than the sum of 3x - 3y + z, 2x - 4y - 8z

In the figure below: Calculate the total surface areas of the two solids.





### Lesson 5

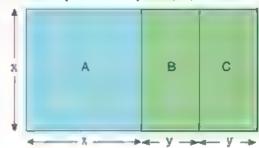
# Multiplying a monomial by an algebraic expression



The following figure on the right is a rectangle made up of three parts, A, B, and C

The dimensions of the rectangle are x and (x + 2y) units.

Therefore, the area of the rectangle  $= x \times (x + 2y)$  square units.

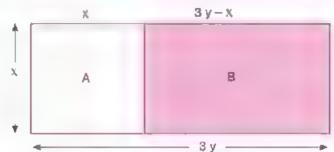


[a] What is the area of the three parts A, B and C?



The figure below is a rectangle made up of two parts A and B, the dimensions of the rectangle are x and 3y units.

[a] Area of A and B together = .....



[b] Area of B = 
$$x (3y - x)$$

### Example (1)

### Multiply

[a] 
$$3(x^2-4x)$$

[b] 
$$2xy(x^2y + 5y^3)$$

Solution:

[a] 
$$3(x^2-4x)=3x^2-12x$$

[b] 
$$2xy(x^2y + 5y^3) = 2x^3y^2 + 10xy^4$$

### Example (2)

**Simplify:**  $5(2x-1)-3(x^2-1)+x(5x-1)$ , then find the numerical value of the expression when x=1

Solution:

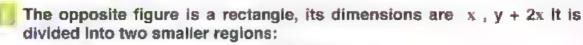
$$5(2x-1)-3(x^2-1)+x(5x-1)$$

The numerical value = 
$$2(1)^2 + (9 \times 1) - 2$$

$$= 10x - 5 - 3x^2 + 3 + 5x^2 - x$$

$$= 2x^2 + 9x - 2$$
  
=  $2 + 9 - 2 = 9$ 

### Exercise (2-5)



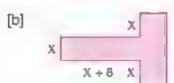
- [a] Calculate the sum of the areas of the two parts.
- [b] Calculate the product of the length and the width of the rectangular region.
- [c] Compare the answers of parts (a), and (b). X
  What are the property of numbers does this diagram illustrate?





🗾 Find the area of each shaded region:







### Simplify:

[a] 
$$4(x-3)$$

[b] 
$$3y(y+5)$$

[c] 
$$2y^2 - y - 5$$
  
×  $2y$ 

[d] 
$$-3(y+3)$$

$$[f] \ 2k^2 - 3k - 7$$

## Simplify:

[a] 
$$\frac{1}{3}$$
 x<sup>2</sup> (6x<sup>2</sup> - 9xy - 3y<sup>2</sup>)

[b] 
$$2x^2y(2x^2-3xy+y^2)$$

**Simplify:** 
$$3(1-2x) - (x^2 - 5x + 3) + 2x(x + 3)$$
, then find the numerical value of the expression when  $x = -2$ 

### Lesson 6

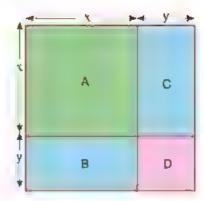
# Multiplying a binomial by an algebraic expression



This square is made up of four parts, A, B, C and D

The sides of the square are each (x + y). therefore the area of the square is  $(x + y)(x + y) = (x + y)^2$  square units





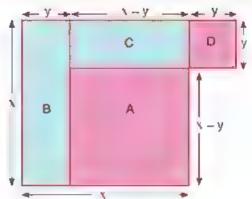
$$(x + y)^2 = \dots$$

Square of a binomial = square of the first monomial +  $2 \times product$  of the two monomials + square of the second monomial.



Area of the square made up of A, B and  $C = X \times X = X^2$  square units.

Therefore, the total area of the figure is  $(X^2 + y^2)$  square units.



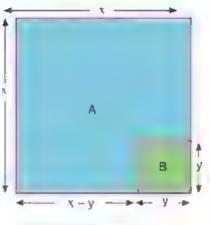
### Complete:

area of 
$$A = \dots$$
 ..... area of  $C = \dots + \dots + \dots$  area of  $B +$ area of  $C +$ area  $D = \dots + \dots + \dots + \dots + \dots + \dots$ 

$$(x - y)^2 = \dots$$
  
 $x^2 + y^2 = (x - y)^2 + \dots$ 

## (6) In the opposite figure:

 A small square B of area y² square units is removed from a bigger square A of area x² square units, therefore
 The area of the remainder = x² - y² square units.



 Suppose the remaining area is cut into two portions then it is rearranged to form a rectangle, as shown:



### Complete:

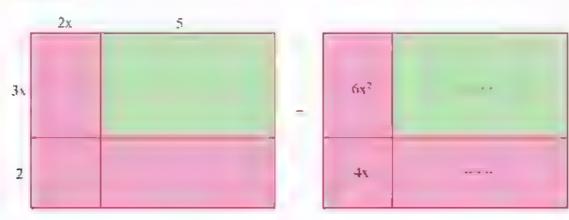
[a] Area of the rectangle = (x + y)(x - y)

[b] 
$$x^2 - y^2 = \dots$$

# 1

The following figure shows the product of two binomials (3x + 2), and (2x + 5) can be thought of as the area of a rectangle as shown in the following diagrams:

### Complete:



$$(3x + 2) (2x + 5) = ... + ... + ... + ...$$

### Horizontal method

$$(3x + 2) (2x + 5) = 3x (2x + 5) + 2 (2x + 5)$$

$$= \dots + \dots + \dots + \dots$$

$$= \dots + \dots + \dots$$

### Vertical method

$$3x + 2$$

$$2x + 5$$

$$6x^2 + 4x$$

$$6x^2 + \dots + \dots$$

### Inspection method

$$(3x + 2) (2x + 5)$$

$$= 6x^{2} + (... + ....) + 10$$

$$= 6x^{2} + .... + ....$$

### Complete:

[a] 
$$(3x + 2)(x + 7) = 3x^2 + \dots + 14$$
 [e]  $(x + 5y)(x - 5y) = \dots$ 

[e] 
$$(x + 5y) (x - 5y) = ...$$

[b] 
$$(3x-2)(x-7) = \dots$$

$$[f](x-4)(x+4) = \dots$$

[c] 
$$(3x-2)(x+7) = \dots$$

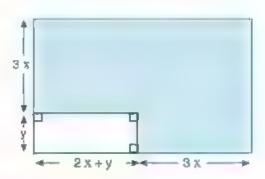
[g] 
$$(2x + y)^2 = \dots$$

[d] 
$$(3x + 2)(x - 7) = \dots$$

[h] 
$$(2x - y)^2 = \dots$$

# In this figure:

What is the area of the shaded part of the rectangle?



### Solution:

	Length	Width	Area
Large rectangle	5x + y	3x + y	(5x + y) (3x + y)
Small rectangle	2x + y	У	(2x + y) y

Shaded area = ...... = ......

### Use the previous methods to find: (x + y) (2x + y + 1)

### Example (1)

### Multiple the following:

$$(a)(2x + 3y)^2$$

$$[b] (5a - b) (5a + b)$$

### Solution:

[a] 
$$(2x + 3y)^2$$
 =  $(2x)^2 + 2x \times 3y \times 2 + (3y)^2$ 

$$= (2x)^2 + 2x \times 3y \times 2 + (3y)^2$$

$$=4x^2+12xy+9y^2$$

[b] 
$$(5a - b) (5a + b) = (5a)^2 - (b)^2$$

$$[c] (m - 7n)^2$$

[c] 
$$(m - 7n)^2 = (m)^2 - m \times 7n \times 2 + (7n)^2$$

$$= m^2 - 14mn + 49n^2$$

### Example (2)

### Multiply, then find the numerical value at x = 2, y = 1

[a] 
$$(x + 9)(x + 2)$$

$$[c] (2x + y) (x + 2y)$$

[b] 
$$(y + 3)(y + 1)$$

#### Solution:

[a] 
$$(x + 9) (x + 2) = x^2 + 11x + 18$$
 at  $x = 2$ 

$$= (2)^2 + 11 \times 2 + 18 = 4 + 22 + 18 = 44$$

[b] 
$$(y + 3) (y + 1) = y^2 + 4y + 3$$
 at  $y = 1$ 

at 
$$y=1$$

$$= (1)^2 + 4 \times 1 + 3 = 8$$

[c] 
$$(2x + y)(x + 2y) = 2x^2 + 5xy + 2y^2$$
 at  $x = 2$ 

$$= 2 \times (2)^2 + 5 \times 2 \times 1 + 2 \times (1)^2$$

$$= 8 + 10 + 2 = 20$$

### Exercise (2-6)

### Simplify Multiply the following:

[a] 
$$(4x + 1)(2x + 3)$$

[b] 
$$(5m-2)(6m+1)$$

[c] 
$$(8x-2)(3x-7)$$

$$[d] (4m - 7)^2$$

[e] 
$$(3x + y)^2$$

$$[f](4m-7)(4m+7)$$

$$[g] (6x - 2y) (6x + 2y)$$

$$[h](-12m + 9)(-12m - 9)$$

## 🫃 Simplify:

[a] 
$$3 (m-5) (m+2)$$

[b] 
$$3a (2a - 5b) (3a + b)$$

[c] 
$$3x (2x + 4y)^2$$

[d] 
$$4(xy-2)^2$$

[e] 
$$(5x - 2y)^2 - (5x + 2y)^2$$

[f] 
$$(2x^2 + 3)(x^2 - 5) - (3x^2 + 2)^2$$

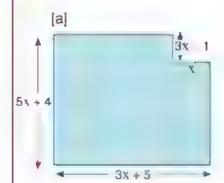
### Select the correct value:

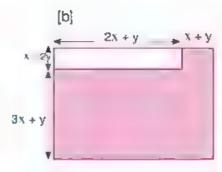
[a] If 
$$(2x + y)^2 = 4x^2 + kxy + y^2$$
, then  $k = ...$  [2, 4, 8]

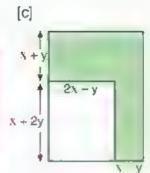
[b] If 
$$(x-y)(2x+y) = 2x^2 + kxy - y^2$$
, then  $k = ...$  [-1, 1, 3]

[c] If 
$$(x-3)(x+3) = x^2 + k$$
, then  $k = ....$  [9, 8, -9]

Write an expression for the perimeter and area of each shaded region:







Multiply then calculate the numerical value of the product by substitution When x = 1, y = -2:

[a] 
$$(2y + 7)(3y + 4)$$

[c] 
$$(x + 4) (3x + 2)$$

[b] 
$$(3x + y)(x + 3y)$$

[d] 
$$(x + 4)^2 (3y + 2)$$

# Simplify:

[a] 
$$(2y+1)(y^2+y+5)$$

[c] 
$$(7n + 2) (2n^2 - 5n + 1)$$

[b] 
$$(4 + 2a + 3a^2)(2 - a)$$

[d] 
$$4x^2 + x - 5$$
  
  $\times x + 6$ 

[a] If 
$$(2-y)^3 = 8 - 12y + 6y^3 - y^3$$
 obtain the value of  $(2-y)^4$ 

[b] Use Mental Math to find the value of:

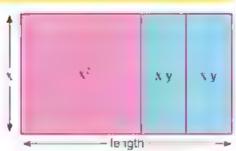
- 1)  $(41)^2$  in the form  $(40 + 1)^2$
- 2)  $(49)^2$  in the form  $(50-1)^2$
- 3) 201  $\times$  199 in the form (200 + 1) (200 1)

# Lesson 7 Dividing an algebraic expression by a monomial

This figure is a rectangle made up of three parts. Area of the rectangle =  $(x^2 + 2xy)$ 

The length of the rectangle =

Area of the rectangle ÷ Width of the rectangle



The length of the rectangle =  $\frac{x^2 + 2xy}{x} = \frac{x^2}{x} + \frac{2xy}{x} = \dots + \dots$ 



[a] The length of the rectangle whose area  $x^2 + xy = \frac{x^2 + xy}{2} = \dots + \dots$ 

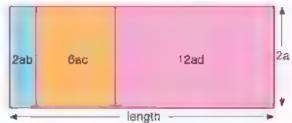
[b] The length of the rectangle whose area  $2xy = \frac{2xy}{x} = \dots$ 

[c] The length of the rectangle whose area  $xy = \frac{xy}{1-x^2} = \dots$ 

[d] The length of the square whose area  $x^2 = \frac{x^2}{10000} = 10000$ 

The following figure is a rectangle made up of three parts, its area is (2ab + 6ac + 12ad)

Length of the rectangle = area ÷ width



### Example

Divide each of the following

(b) 
$$\frac{9l^{4} m^{4} - 18lm^{4}}{3 l m^{2}}$$

Solution:

[a] 
$$\frac{26 e^2 + 14 e^4}{2 e} = \frac{26 e^2}{2 e} + \frac{14 e^4}{2 e} = 13 e + 7 e^3$$

(b) 
$$\frac{9 l^3 m^4 \cdot 18 l^4 m^4}{3 l^4 m^2} = 3 l^2 m^2 - 6 m^2$$

### Exercise (2-7)

The symbols in the following monomials and algebraic expressions represent non - zero numbers.

Complete:

[a] 
$$\frac{18a^5b^2}{6a^2} = \frac{18}{6} \times \frac{a^5}{a^2} \times \frac{b^2}{1} = ....$$

[b] 
$$\frac{15n^3 - 9m^4n^2}{-3n^2} = \frac{15n^3}{-3n^2} + \frac{-9m^4n^2}{-3n^2} = \dots + \dots$$

[c] 
$$\frac{12x^3 - 8x}{4x} = \frac{12x^3}{4x} \cdot \frac{8x}{4x} = \cdots$$

$$[d] \ \frac{16x^4\,y^2 - 12x^3\,y^3 + 24x^2\,y^4}{8x^2\,y} = \frac{16x^4\,y^2}{8x^2\,y} - \frac{16x^2\,y}{8x^2\,y} + \frac{16x^2\,y}{8x^2\,y} = .... + ....$$

Find the quotient in each case:

[a] 
$$\frac{18a^2}{3a}$$

$$[d] \, \frac{18x^4\,y^5 - 42x^5\,y^4}{-6x^2\,y^2}$$

[b] 
$$\frac{18m^4 + 32m^2}{-2m^2}$$

[e] 
$$\frac{24x^4 - 16x^3 - 42x^2}{6x^2}$$

$$[c] \frac{48x^3 - 80x^2}{8x^2}$$

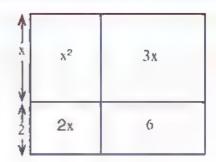
[f] 
$$\frac{32x^5 - 48x^3 + 72x^7}{-8x^3}$$

### Lesson 8

# Dividing an algebraic expression by another one

### In the opposite figure:

A model of peice of land rectngular shape its area  $(x^2 + 5x + 6)$  m<sup>2</sup> and its width is (x + 2) m, find its length to get the length of the rectangle you have to find the quotient of  $x^2 + 5x + 6$  by x + 2



### Solution:

[a] Rearrang the dividend (x² + 5x + 6) and the divisor (x + 2) according to the desendingly powers of x.

$$x^2 + 5x + 6 \quad x + 2$$

$$\rightarrow$$
 " $x^2 + 2x$   $x + 3$ 

$$\rightarrow$$
 3x + 6

the final subtraction equals zero

: The quotient = x + 3 the length of the rectangle

### Example (1)

Find the quotient of  $x^3 + 1$  by x + 1

### Solution:

. The quotient =  $x^2 - x + 1$ 

### Example (1)

Find the value of k which makes the expression

$$2x^3 - x^2 - 5x + k$$
 is divisible by  $2x - 3$ 

Solution:

.. 
$$k - 3 = 0$$
  $\rightarrow k = 3$ 

### Exercise (2-8)

### Find the quotient of each of the following:

[a] 
$$2x^2 + 13x + 15$$

[b] 
$$3x^3 - 4x + 1$$

[c] 
$$3x^2 + x^3 - x - 3$$

[d] 
$$x^4 + 3x^2 + 2$$

by 
$$x^2 + 1$$

[e] 
$$x^4 + 49 \cdot 18 x^2$$

by 
$$2x - 7 + x^2$$

[f] 
$$x^3 - 27$$

### Find the value of k which makes the expression

[a] 
$$x^3 - 3x^2 - 25x + k$$
 is divisible by

$$x^2 + 4x + 3$$

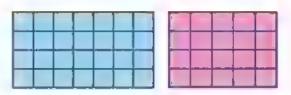
[b] If the area of rectangle is  $(2x^2 + 7x - 15)$  and its length is (x + 15). Find its width and its perimeter at x = 3cm

### Lesson 9

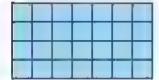
# Factorization by Identifying the highest common factor (H.C.F.)

Draw a rectangle whose dimensions are 7, 4 units on a squared paper, and a rectangle whose dimensions are 5, 4 of the same units.

Calculate the area of the two rectangles by two different methods.



#### First method

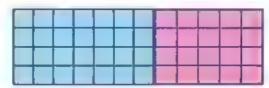




Area of rectangles =  $(4 \times 7) + (4 \times 5)$ 

= .... + .... = ......

### Second method



Area of rectangles = 4 x (7 + 5)

= 4 x .... = .....

### Note that

 $4 \times (7 + 5) = (4 \times 7) + (4 \times 5)$  means that we used distributing multiplication on addition, while  $(4 \times 7) + (4 \times 5) = 4 \times (7 + 5)$  means factorization by identifying the H.C.F. between the two terms  $(4 \times 7)$  and  $(4 \times 5)$ , which is 4. Each of 4, (7 + 5) is called a factor of the expression 4 (7 + 5)

Generally: ab + ac = a(b + c)

### Example (1)

Factorize by identifying the H.C.F. of the expression:

$$3x^2y^3 - 9x^3y^4 + 12x^3y^2$$

### Solution

The H C.F. =  $3x^2 y^2$ 

### Example (2)

Factorize by identifying the H.C.F. of the expression:

#### Solution

The H.C.F. = (4a + 5b)

To find the other factor, we divide each term by the H.C.F.

$$3x^2y^3 - 9x^3y^4 + 12x^3y^2$$

$$= 3x^2 y^2 (y - 3x y^2 + 4x)$$

$$3a (4a + 5b) - 2b (4a + 5b)$$
  
=  $(4a + 5b) (3a - 2b)$ 

### Exercise (2-9)



### Factorize by identifying the H.C.F.:

[a] 
$$3x^2 + 6x$$

[b] 
$$8y^2 - 4x^2$$

$$[e] 49b^2 - 7b^3$$

$$[f] 3x^2 + 12x - 6$$



### Factorize by identifying the H.C.F.:

[b] 
$$9m^4 n^2 - 6m^3 n^3 + 12m^2 n^4$$

[c] 
$$18a^2$$
 bc  $-6abc + 30abc^2 - 24ab^2$  c<sup>2</sup>

[d] 
$$-2x^{5} + 4x^{2} - 6x + 2x^{3}$$

$$[1] 3x (a+b) + 7 (a+b)$$

[f] 
$$(x + 4) x^2 + (x + 4) y^2$$

[g] 
$$3x^2(x-7) + 2x(x-7) + 5(x-7)$$

[h] 
$$4m^2(2x + y) - 3m(2x + y) - 7(2x + y)$$

### ...

### Find the result by identifying the H.C.F.:

[b] 
$$6 \times 15^2 + 18 \times 15 - 8 \times 15$$

### Miscellaneous Exercises



### Circle the correct answer:

[a] If a = 0, b = 5, and c = 2, then the numerical value of  $a^2 b + ac$  equals .....

[0, 2, 6, 8]

[b] If the price of 4 shirts is L.E.X., then the price of 40 shirts is . . . .

 $[10x, \frac{x}{40}, \frac{5x}{2}, \frac{40}{4}]$ 

[c] If  $\frac{a}{b} = 70$ , then  $\frac{a}{2b} = ....$ 

[35, 68, 72, 140]

[d]  $7x^2 + 14y^2 = 7$  (.....)

 $[x^2 + y^2, x^2 + 2y^2, 7x^2 + y^2, x + 2y]$ 

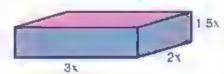
[e]  $(15x^4 + 5x^3) \div 5x^8 = \dots$ 

 $[3x^2 + x \cdot 5x^2 + 1 \cdot 3x + 1 \cdot 4x^4]$ 

[f]  $\frac{3x}{7} - \frac{x}{7} = \dots$ 

 $[\frac{2}{7}, \frac{x}{7}, \frac{2x}{7}, 2x]$ 

[g] The volume of the cuboid is .. ...



[6.5x , 2 (5x) (1.5x) , 9x<sup>3</sup> , 2 (4.5x<sup>3</sup>)]

[h] If x = 4, y = 6, and z = 24, which of the following is true?

$$[x = \frac{z}{y}, x = \frac{y}{z}, x = yz, x = y + z]$$

### Complete:

[a] The degree of the term 3x2 y is ..., . and its coefficient is . ....

[b] 
$$6a^2 + 12 ab = 3a ( ... + ....)$$

[c] 
$$x (a + 1) - y (a + 1) = (a + 1) (....$$

[d] 
$$(4a^2 + 2a) \div 2a = \dots$$

[e] 
$$7 + 7^2 + 8 + 8^2 = \dots \times 8 + \dots \times 9$$

[f] 
$$(31)^2 \approx 901 + 2 \times \dots \times \times \dots$$

[g] 
$$(20 + 1)$$
  $(20 - 1) = 400 - \dots$ 

[h] The seventh term in the pattern:  $\frac{1}{10000}$ ,  $\frac{1}{1000}$ ,  $\frac{1}{100}$ , ...... is .....

### Simplify to simpliest form:

[b] 
$$3x^2 + 5x^3 + x^2 + 2x^3$$

[d] 
$$2x (3x + y) + 3y (x + y)$$

### Use two methods to simplify:

$$[a] \frac{X^3 + Xb^2}{Xb}$$

[b] 
$$\frac{19^2-2 \times 19+19}{19}$$

### Write the product:

[a] 
$$(2x - 5y) (2x + 5y)$$

[d] 
$$(x - 3y)^2$$

[b] 
$$(2x - 5y) (2x - 5y)$$

$$[m] (2x - y)^2$$

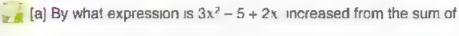
[c] 
$$(x + 1) (x^2 - x + 1)$$

$$[f](3a - 5b)(2a + 7b)$$

### Factorize by identifying the H. C. F.:

[a] 
$$16x^3 + 8x^2$$

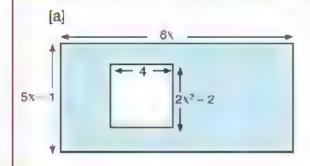
[d] 
$$5(48)^2 + 7 \times 48 + 53 \times 48$$

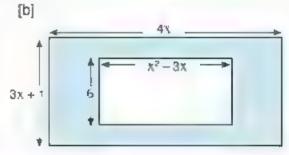


$$x + 5x^2 + 1$$
 and  $2x^2 - 4 - 2x$ 

[b] Simplify: 2n (n + 5) + n (6 - n), then calculate the numerical value when n = -1

### Find the area of the shaded region:





[a] If a = 4x - 3, b = 2x + 1, and c = 3x - 2. Find in terms of x the value of the expression:  $ab - c^2$ 

[b] Multiply: (x - 2y) (x + 2y) by  $(x^2 + 4y^2)$ 

### Complete:

[a]  $5x^2 + 3$  is an algebraic expression of the ..... degree.

[b] 
$$(2x-1)^2 = ... - 4x + 1$$

[c] 
$$a^2 b + b^2 a = ..... (a + b)$$

[d] 
$$(x-5)$$
 (......) =  $x^2-25$ 

### Circle the correct value:

[a] The Algebraic term 2x3 has ....... factors.

[2, 3, 4, 5

[4xy, 2xy, 2x, 2y]

[c] If 2b is the length of a cube then its volume equals ...... [4b<sup>2</sup>, 2b<sup>3</sup>, 4b<sup>3</sup>, 8b<sup>3</sup>]

[d] This figure is a rectangle with dimensions 2a, 3b then its perimeter is ......[6 ab , 2a + 3b , 4a + 6b , (2a + 3b)2]



3b

[e] The factorization of  $6x^2y - 4x$  by identifying the H.C.F. is ........

$$[3xy(x+y), 2xy(3y-2), 2xy(3x-2), 2x(3xy-2)]$$

Find the quotient of each of the following:

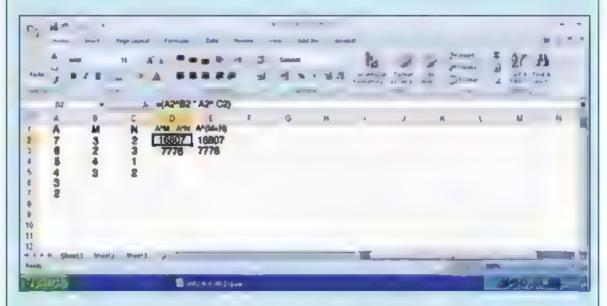
[a] 
$$x^2 + 3x + 2$$

[b] 
$$37x^2 - 4 - 9x^4$$
 by  $3x^2 - 2 + 5x$ 

$$3x^2 - 2 + 5$$

### Activity (1):

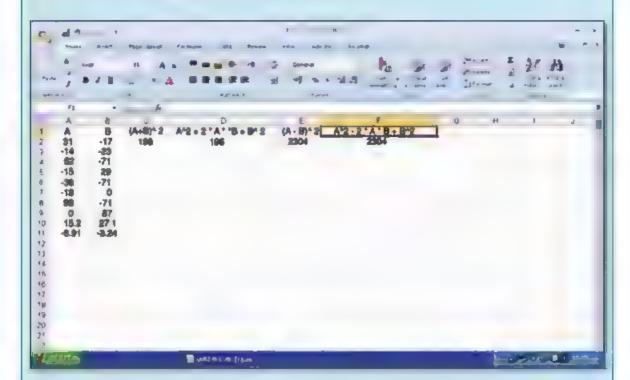
Use the spreadsheet "Excel" to verify the law:  $a^n \times a^n = a^{n+n}$  applies to indices



- Extend your spreadsheet up to row 15 using other positive values of a , m , and n
- Does the law produce consistent outcomes?
- Does the law apply to negative bases (a < 0)?</li>
- Use the same method to venty the law a<sup>m</sup> + a<sup>n</sup> = a<sup>m-n</sup>, m ≥ n, and a > 0
- Does the law apply to negative bases (a < 0)?</li>
- Attach a printed copy of your completed spreadsheet to show your work.

### Activity (2):

Copy the following table on a spreadsheet (Excel):



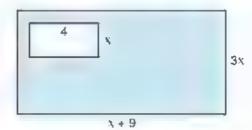
- [c] Extend your spreadsheet up to row 15 with numbers of your choice, and then complete columns C to F Describe your observations.
- [a] Using a similar table as in question 1, verify that  $a^2 b^2 = (a + b)(a b)$ [b] Have a copy of your work.

### **Unit Test**



### Complete:

- [a]  $(x + 5) (x + .....) = x^2 + ..... + 15$
- [b]  $(2x + 1)^2 = 4x^2 + \dots$
- [c] Sometimes a product of 101 x 99 can be found quickly by multiplying two binomials (100 + 1) (.....)
- [d] If a = 2b and b = 15, then the numerical value of a + 2b + 5 is ...
- [e] If a + 3b = 7, and c = 3, then the numerical value of a + 3 (b + c) is . ....
- [f] The area of the shaded region is ...... square units.





### Circle the correct value:

- [a]  $3a^4$  b x  $5a^2$  b<sup>2</sup> x  $2a^3$  = ...
- [60 a<sup>11</sup> b<sup>3</sup>, 30 a<sup>10</sup> b<sup>2</sup>, 150 a<sup>10</sup> b<sup>3</sup>, 30 a<sup>9</sup> b<sup>3</sup>]
- [b] The cube of the sum of a and b is .......
- $[a^3 + b^3, (a + b)^3, a^3 b^3, 3a^3 b^3]$

- [c] (4x-3)(x-4) = ...  $[4x^2-19x-12, 4x^2-7, 4x^2-12, 4x^2-19x+12]$
- [d] If the lateral area of a cube is 36x², then its side length equals.......
- [9x, 9, 3x, 3]

[e]  $(x-2)(x^2+2x+4) = \dots$ 

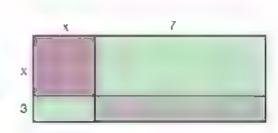
 $[x^3 + 8, x^3 - 8, 3x + 6, x^3 + 6]$ 

[1]  $(x^2 + x) \div x = \dots$ 

 $\{0, x, 2x + 1, x + 1\}$ 



- [3] [a] If a = 3x 4, b = x + 2, and c = 2x 3calculate the numerical value of ab - c2 when x = 0
  - [b] This figure is a rectangle made up of 4 parts, write an algebraic expression which represents the area of the rectangle





[a] 3x4 is an algebraic term of the degree 4	
[b] The algebraic terms $7x^2$ , and $2x^7$ are like terms	
[c] The algebraic expression 3xy + 5 is of the second degree	
[d] $2x - 3y$ is the additive inverse of $3y - 2x$	
[ $\theta$ ] $b^3 = 3 \times b \times b$	

$$[f] (x + 2)^2 = x^2 + 4$$

[a] Divide 
$$x^3y - 4xy^2 + 6xy$$
 by xy

[b] Find the result by identifying the H.C.F.

[a] Subtract 
$$5x^2 + y^2 - 3xy$$
 from  $x^2 - 2xy + 3y^2$ 

[b] Simplify: 
$$(7x y - 3x)^2 - (5x y - x)^2$$

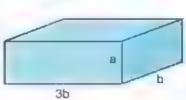
# Calculate the numerical value of the following using substitution when a = -1, b = 2:





$$1) (99.1)^2$$

[b] Two metal cuboids with dimensions as shown were melted and reshaped to a new cuboid with the height (a + b). Calculate the area of its base.



### Find the value of K which makes:

(a) 
$$6x^3 - 13x^2 - 13x + K$$
 is divisible by  $3x - 5$ 

[b] 
$$x^3 - 3x^2 - 25x + K$$
 is divisible by  $x^2 + 4x + 3$ 

# **Statistics**

### Carl Friedrich Gauss (1855 – 1777)

The methods, theories and applications of statistics have been developed by a large number of scientists who discussed its theories and constructed them on sound scientific bases. Among those mathematicians is the german mathematician Carl Friedrich Gauss.



### Contents

Lesson Arithmatic mean

Lesson 2: Median

Lesson 3: Mode

Activity.

# **Measures of Central Tendency**

**Arithmatic mean** 

Median

Mode

First Term 6:

### Lesson 1 Arithmatic Mean

Given the phenomena around us and the values that the different elements of these phenomena take it.

We note that most of the values of these phenomena are closed to each other, this means that they gather around a certain value for example the heights of the students of your class, we find that there is a height which mediates virtually all the heights also the weights of the students of your class and any other phenomenon and there are several statistics measures for measuring the data towards the centre (the mean, the median and the mode).

### 1- The Arithmetic Mean

### Example:

Ahmed goes to his school from Sunday to Thursday, his father gives him pocket money as follows: 6, 4, 7, 3 and 5 pounds. What is the fixed pocket money that Ahmed can take from his father such that he takes the same amount of money.

#### Solution:

The sum of what Ahmed take = 6 + 4 + 7 + 3 + 5 = 25

Numbers of days for going school = 5

The daily = 
$$\frac{25}{5}$$
 = LE 5

The value 5 pounds is called the arithmetic mean for the values 8, 4, 7, 3, 5

### This means:

Note: In the previous Example:

We note that the arithmetic mean is that value which if Ahmed take it in the 5 days, the following satisfies:

Ex (2) : Find the value of x, if the arithmetic mean of the values 8 , x , 7 , 5 is 6

Solution:

The sum of the values = the arithmetic mean x their number

Then: 
$$8+x+7+5=6x4$$

$$20 + x = 24$$

Then: 
$$x = 24 - 20 = 4$$

### Exercises

### 1- Complete:

- (a) The arithmetic mean for the values 18, 35, 24, 6 is .....
- (b) If the arithmetic mean for the numbers 3, 5, x is 4, then x = ..............
- (c) If the sum of 5 numbers is 30, then the arithmetic mean for these numbers = ........
- 2- Find the arithmetic mean for each group of the following:
  - (a) 4 , 6

- (b) 3,5
- (c) 3, 4

(d) 2, 4, 6

- (e) 1,3,5
- (f) 1, 2, 3, 4, 5

(g) 6, 10

- (h)  $\frac{1}{2}$ , 1
- (1) 10, 20

- (j) 35,50,60,55
- 3- If the temperatures for a full week in one of the cities in December month 25°, 27°, 31°, 23°, 22°, 22°, 18°. Calculate the arithmetic mean for these degrees.
- 4- If the number of hours at studying for one of the students during 6 consecutive days:

The day	Saturday	Sunday	Monday	Tuesday	Wednesday
Number of studying hours	3 1/2	3	2 1/2	3	4

Find the mean of studying hours.

5- If the marks of Shrief in 3 consecutive months in maths test as: 89, 91, 96

Calculate the monthly mean for this student.

### Lesson (2)

#### The Median

The median for a set of data is that value which lies exactly in the middle of the set after the ascendingly or descendingly of the elements of this set.

This means that the value of the median divides the given data into two parts such that the number of values greater than the median equals number of the values smaller than it.

Ex. A set of 7 students, their marks in one of the tests are 13, 17, 15, 11, 18, 20, 14, what is the median mark for these students.

#### Solution:

The order of marks (ascendingly)

The median mark = 15

#### The order of the median:

(a) If the number of the values (n) is an odd, then the order of the median is \(\frac{n+1}{2}\) after the arrangement of the data ascendingly or descending in the previous example. Number of values = 7

The order of the median =  $\frac{7+1}{2}$  = 4

(b) If the number of the values is an even, then the order of the median is π/2 and the next.
 i.e. π/2, π/2 + 1 and the value of the median in this case is the mean for these two values as in the example.
 Find the value and the order of the median for the values

: 3 , 1 , 6 , 5 , 2 , 9.  
the order is 9 , 6 , 
$$\boxed{5}$$
 ,  $\boxed{3}$  , 2 , 1  
The order of the median =  $\frac{6}{2}$  ,  $\frac{6}{2}$  + 1

# i.e. the third, fourth, the value of the median = $\frac{5+3}{2}$ = 4

#### Notes:

- If n is an odd (not divisible by 2), then n + 1 is an even, divisible by 2.
- Generally the value of the median ≠ the order of the median.
- The order of the median is always positive integer but the value of the median may be fraction or negative integer according to the given data.

#### Exercises

#### 1- Choose the correct answer :

- (c) If the median for the values a+3, a+2, a+4, where  $a\in Z+$  is 8,

then a = ...... (2, 3, 4, 5)

#### 2- Find the median of each group of the following:

- (a) 3, 5, 12, 11, 8
- (b) 3, 5, 12, 11, 8, 10
- (c)  $\frac{1}{2}$ ,  $\frac{1}{4}$ , 1
- (d) -2 , 0 , -1 , 1 , 5

### 3- The following table shows the marks of Ghad in one Maths test in 6 months.

The month	Oct.	Nov.	Dec.	Feb.	March	April
The mark	41	35	47	37	44	48

Find: (a) The median for the previous marks

(b) The mean for the previous marks.

#### Lesson 3

### The Mode

- The mode is the most common value in the set or in other words, it is the value which is repeated more than any other values.
- The mode as one of the central tendicy measurements is available for the numerical and described values.

Example (1): The following data represents the ages of a set of persons 33, 20, 30, 25, 33, 48, 33, 25, 33, 20.

Find the mode for these ages.

Solution: The mode = 33

Find the mode for this set.

Solution: The mode for this set is (B)

#### Remarks:

If all the given values are different, then there is no mode for these values.

Example: 23, 25, 48, 57, 19, 33, 32 (data)

Some values have more than one mode.

**Example**: 9,7,7,7,5,5,4,4,4,3,2 there is two modes for this set of values which are 7 and 4 (set of two modes) (we will study the data with only one mode)

#### Exercises

- (a) The mode for the set of values: 14, 11, 12, 11, 14, 15 and 11 is ......
- (b) The mode for the colors red, yellow, red, white, black, red and white is .....
- (c) If the mode for the values 15, 9, x + 1, 9, 15 is 9, then  $x = \dots$

#### 2- Choose the correct answer:

- (a) The mode for the values 1, 3, 7, 3, 6, 7 and 3 is . . . . . . . . [1, 3, 6, 7]
- (b) If the mode for the following set of values 7, 5, y + 3, 5 and 7 is 7, then y = ... .......

[3,4,5,7]

### 3- Find the mean, median and the mode for the following values:

## The activity of the unit

(1) Which of the following numbers is the arithmetic mean for the other values?

(a) 26

(b) 28

(c) 29

(d) 30

(e) 37

- (2) If the mean of Karem's marks in 5 tests is 84, the mean of his marks in the first three tests is 80, then what is the mean of his marks in the last 2 tests?
- (3) Calculate the mean and the median for each set of the following sets of numbers:

(a) 1, 2, 3, ...., 8, 9, 10

(b) 1, 2, 3, ...., 9, 10, 11

(c) 1, 2, 3 ....., 99, 100

(d) 1, 2, 3, ...., 100, 101

(e) 0, 2, 4, 6, 8, 10

<sup>\*</sup> Does each of the previous sets have a mode or not?

## **Geometry and measurement**

#### **Euclid**

(325 BC - 265 BC)

Euclid is a Greek Mathematician Scientist, He lived in Alexandria, is considered the father of Geometry, he said that "What made without evidence can be refused without evidence"

#### Definitions:

The point is what it is not part.

The straight line has neither length not width. Some axioms:

A straight line segment can be drawn by joining any two points.

A straight line segment can be extended indefinitely in a straight line.

All right angles are equal.



#### CONTENTS

Lesson 1 Geometric Concepts.

Lesson 2 Congruence

Lesson 3 Congruent triangles

Lesson 4 Para lelelism

Lesson 5 Geometric constructions

Unit test

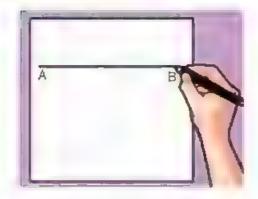
#### Lesson 1

## Geometric concepts

### The line segment

Mark two points on a sheet of paper which is a representation of a plane in geometry.

If we join them with a straight edge, we have a line segment. The two points we joined are called end points. IF we name these two points A and B, we get a line segment AB is written as  $\overline{AB}$  or  $\overline{BA}$ .



### The straight line

indefinitely, we will get what we call, in geometry, a straight line. A straight line AB, Written as AB, or BA.

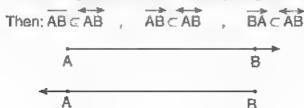
There is an infinite number of points on the straight line, the arrows show that the line can be extended without limit on both sides



### The ray

If we extend the line segment AB in either direction indefinitely, we will get a ray AB, or a ray BA.

Ray AB is written as AB, where the ray starts at A and continuous without end from A through B in a straight line so it is infinitely long. Thus its length is not determined.



## The angle

We can view an angle as the rotation of a ray from one position to another around the starting point.



C

If A, B and C or three non-collinear points then  $\overrightarrow{AB}$ ,  $\overrightarrow{AC}$  form the angle BAC and is written as  $\angle$  BAC ,  $\overrightarrow{AB}$   $\bigcup$   $\overrightarrow{AC}$  =  $\angle$  BAC

The angle is the union of two rays with the same starting point.

The common point of the two rays is called the vertex of the angle.

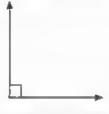
Each of the two rays is called a side of the angle.

The angle divides its plane into three sets of points which are:

- The angle.
- The interior of the angle.
- The extelor of the angle.

## Types of angles

Angles are classified according to their measures as follows



An angle of 90° is called a right angle



a straight angle is an angle whose measure is 180°



An angle of less than 90° But is greater than Zero° is called an acute angle



An angle that is greater than 180° but less than 360° is called a reflex angle

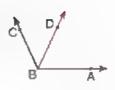


An angle of greater than 90° but less than 180° is called an obtuse angle

Zero ang e is an angle whose measure is zero, where its sides are coincident

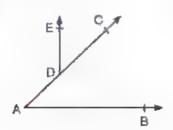
## Some relations between the angles Adjacent angles

Two angles are said to be adjacent if they have a common vertex, a common side and the other two sides are on opposite sides of the common side.

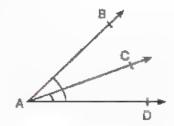


∠ABD, ∠DBC are adjacent

### Notice that:



U

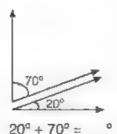


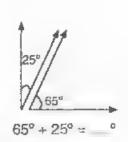
∠BAC and ∠EDC are not adjacent because they have not a common vertex ∠BAC and ∠BAD are not adjacent because the sides AC and AD are not on the opposite sides of AB

## Complementary angles

Suppose we are given two pairs of angles, 25°, 65° and 70°, 20°.

What do you notice about the sum of each pair of angles?





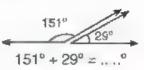
Two angles are said to be complementary if their sum is 90°.

## Supplementary angles

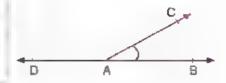
We are given two pairs of angles, 125°, 55° and 151°, 29°.

What do you notice about the sum of each pair of angles?





Two adjacent angles formed by a straight line and a ray with a starting point on this straight line are supplementary

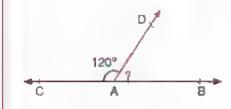


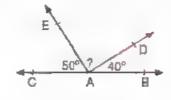
 $m (\angle BAC) + m (\angle CAD) = 180^{\circ}$ 

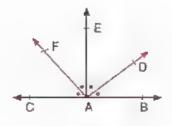
Dirl

In each of the following figures:

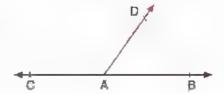
If A E BC , then complete:







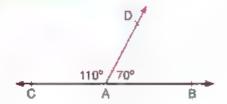
Draw the two adjacent angles BAD and DAC such that the sum of their measures is 180°. Repeat this work, what is the relation between AB and AC?

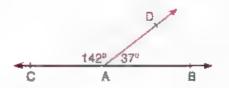


If two adjacent angles are supplementary then their outer sides are on the same straight line.

AB and AC are on the same straight line.

### Example (1)



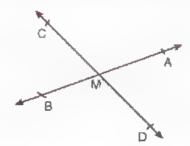


AB and AC are on the straight line because m (∠BAC) + m (∠DAC) = 180°

AB and AC are not on the same straight line because m (∠BAD) + m (∠DAC) ≠ 180°

### vertically opposite angles

Draw AB and CD to intersect at M, then measure the angles: AMC, CMB, BMD, and DMA what do you notice?



If two straight lines intersect, then the measures of each two vertically opposite angles are equal.

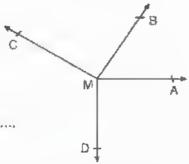
## Accumulative angles at a point

From the point M, Draw
MA, MB, MC, MD, then measure

the resulted adjacent angles.

 $m (\angle AMB) + m (\angle BMC) + m (\angle CMD) + m (\angle DMA) = ....$ 

Repeat this work, what do you notice?

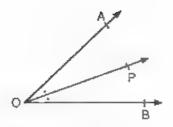


The sum of the measures of the accumulative angles at a point is 360°

## Angle bisector

An angle bisector is a ray that divides an angle into two halves

OP divides ∠AOB into two angles having the same measure and OP is called the b sector of ∠AOB.



#### Example (2)

In the figure opposite,

M is the point of intersection of AB and CD, ME bisects

∠AMC, and m (∠BMC) = 116°

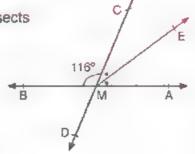
Find: m (∠AMC), m (∠AMD), and m (∠AME)



$$m (\angle AMC) = 180^{\circ} - 116^{\circ} = 64^{\circ}$$

$$m (\angle AMD) = m (\angle CMB) = 116^{\circ} v. opp. angles$$

m (
$$\angle AME$$
) =  $\frac{1}{2}$  m ( $\angle AMC$ ) =  $\frac{64^{\circ}}{2}$  = 32°



## Example (3)

In the figure opposite,

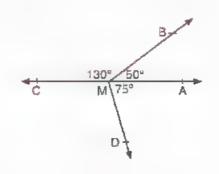
### Complete:

(2) .... and .... lie on the same straight line.

## Solution:

(1) m (
$$\angle$$
CMD) = 360° - (50° + 130° + 75°) = 105°

(2) MA and MC lie on the same straight line



### Exercise (4-2)

#### Complete:

- [a] If m ( $\angle A$ ) = 80° then m (reflex  $\angle A$ ) = .....°
- [b] The measure of each of two equal complementary angles equals ... .º
- [c] If  $\angle A$  and  $\angle B$  are supplementary angles and m ( $\angle A$ ) = 2 m ( $\angle B$ ) then m ( $\angle B$ ) = ... °

### 🗾 Draw an angle PQR:

- [a] Measure ∠PQR.
- [b] Draw ray QS between QR and QP such that m ( $\angle$ SQR) =  $\frac{1}{2}$  m ( $\angle$ PQR).
- [c] Does QS bisect ∠PQR?

[d] Produce RQ to T

- [e] Draw the bisector QU of ∠PQT Measure the angles first before answering (f) and (g).
- [f] Name all pairs of complementary angles.
- [g] Name all pairs of supplementary angles.
- [a] Use your protractor to draw angles which have the values
  - [a] 60°
- [b] 115°
- [c] 195°
- [d] 245°

Classify the angles into acute, obtuse and reflex angles.

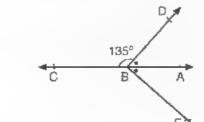
- [b] What are the supplements of the angles whose measures are?
  - [a] 10°
- [b] 117°
- [c] 82°
- [d] 92 1º
- [c] What are the complements of the angles whose measures are?
  - [a] 37°
- [b] 48°
- [c] 45°
- [d]  $22\frac{1}{2}^{\circ}$

## in the figure opposite,

If  $B \in AC$  ,  $m (\angle DBC) = 135^{\circ}$  and

BA bisects ∠DBE find:

m (∠ABD), m (∠DBE), m (∠CBE)



### In the figure opposite,

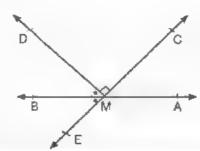
If AB \(\cap \text{CE} = \{\text{M}\},

MD \_ CE and MB bisects

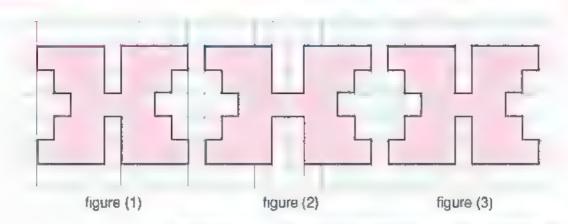
∠DME find:

m (∠BME), m (∠DME),

m (∠AMC) and m (∠AME)



## Lesson 2 Congruence



Using the design shown above,

#### Complete the following:

If you trace the figure, you will find figures ....., ...... have the same size and shape, but the figure ..... is slightly wider

Two figures are congruent if there is a correspondence between the vertices such that each side and each vertex of one coincides with the corresponding element of the other.

Two line segments are congruent if they have the same length.

Two angles are congruent if they have the same measure.

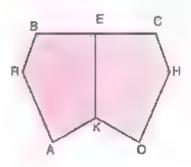
 The polygon BRAKE is congruent to the polygon CHOKE, the vertices are written in the same order.

### Complete:

$$m(\angle C) = m(\angle ....), m(\angle OKE) = m(\angle ....)$$

$$m (\angle H) = m (\angle .....), m (\angle KEC) = m (\angle .....)$$

$$m(\angle O) = m(\angle ...)$$



### Exercise (4-2)



In the Figure: there is one leave differs from the others. Which one is different and how?





The two pentagons shown are congruent.

#### Complete

- [a] B Corresponds to ......
- [b] The polygon BLACK is congruent to the polygon......

$$[d] m (\angle E) = m (\angle .....)$$

[f] 
$$m(\angle A) = m(\angle .....)$$

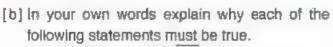


In the figure opposite.

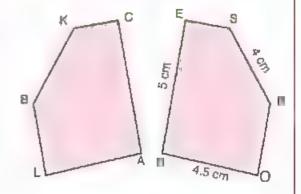
OR is the axis of symmetry of NERAM, O ∈ NM

### [a] Complete

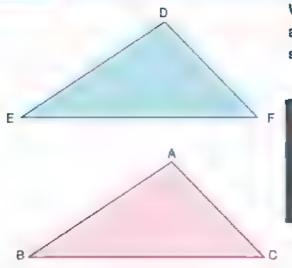
- . The quadrilateral NERO is congruent to the quadrilateral ......
- The common side of the two congruent quadrilaterals is ......



- 1. O is the mid-point of NM.
- 2. ∠NOR is congruent to ∠ M O R
- 3. RO L NM
- 4. OR in the polygon MARO is congruent to OR in the polygon NERO.



## Lesson 3 Congruent triangles



We know that any triangle has three sides and three angles, which are known as the six elements of the triangle.

Two triangles are congruent, if each of the six elements of one coincides with the corresponding element of the other triangle.

We can usually decide whether two thangles are congruent by placing  $\triangle$  ABC on top of  $\triangle$  DEF to see if they fit (Sometimes we may have to flip one of the triangles over). The vertices like will watch

$$A \longleftrightarrow D$$

The sides and angles will also match:

Corresponding angles

Corresponding sides

The symbol "  $\equiv$  " is used as a short form for " is congruent to " thus  $\triangle$  ABC  $\equiv$   $\triangle$  DEF " is read as triangle ABC is congruent to triangle DEF.

Asimple way to remember the correspondence is shown below.

We should not write

We can write △ BCA ≡ △ EFD

$$\triangle CAB \equiv \triangle FDE$$

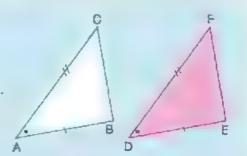
\* \*

#### **Congruent Triangles**

- To test whether two triangles are congruent, or not you don't need to test all the three sides and the three angles.
- Instead of using your geometrical instruments, you can draw and measure figures on your computer to help you discover some rules about congruent triangles.

## Activity 11:

\* Draw any △ ABC and △ DEF such that: m (∠FDE) = m (∠CAB), DE = AB and DF = AC. Measure BC, EF, ∠ABC and ∠DEF, What do you notice?



 Vary △ ABC and △ DEF (Make sure that the above three given conditions are satisfied.)

Move  $\triangle$ DEF and check whether it falls exactly onto  $\triangle$  ABC is this sufficient so as  $\triangle$  ABC  $\equiv$   $\triangle$  DEF?

The first case.

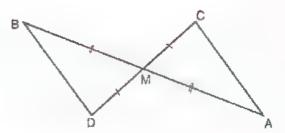
#### Two sides and the included Angle' test (SAS).

Two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle.

#### Example

In the figure opposite,

AB  $\cap$  CD = {M}, AM = BM, and CM = DM. Does  $\triangle$  AMC  $\equiv$   $\triangle$  BMD? why?



#### Solution:

from the figure: AM = BM, CM = DM,  $m (\angle AMC) = m (\angle BMD) v.opp. angles then <math>\triangle AMC \equiv \triangle BMD$ 

## Activity 2:

★ Draw any ABC and DEF such that.

AB=DE

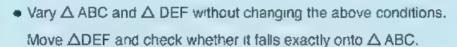
 $m (\angle CAB) = m (\angle FDE)$  and

 $m (\angle CBA) = m (\angle FED).$ 

Measure AC, DF, BC, EF,

ZACB and ZDFE.

What do you notice?





#### Two angles and a corresponding side' test (ASA).

Two triangles are congruent if two angles and the side drawn between their vertices of one triangle are congruent to the corresponding parts of the other triangle.

#### Dirli

In the figure opposite,

Complete:

△ ABC = .....

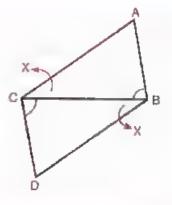
Why?

From the results of congruency:

$$m(Z.A) = m(Z.....),$$

84

... = BD



## Activity 3:

★ Draw any △ABC and △DEF such that AB = DE, DF = AC and EF = BC. Measure ∠CAB, ∠FDE, ∠ABC, ∠DEF, ∠ACB and ∠DFE What do you notice?





 Vary △ ABC and △ DEF (Make sure that the above three given conditions are satisfied.)

Move  $\triangle$ DEF and check whether it falls exactly onto  $\triangle$  ABC is this sufficient so as  $\triangle$  ABC  $\equiv$   $\triangle$  DEF?

The third case

#### Side-Side-Side' test (SSS).

Two triangles are congruent if each side of one triangle is congruent to the corresponding side of the other triangle.

#### Example

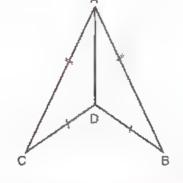
In the figure opposite,

 $AB = AC \cdot BD = CD$ 

verify that: AD bisects ∠A

#### Solution:

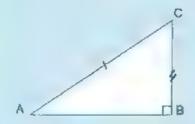
 $\triangle$  ABD  $\equiv$   $\triangle$  ACD (sss) From the results of congruency then m ( $\angle$ BAD) = m ( $\angle$ CAD) i.e AD bisects  $\angle$ A

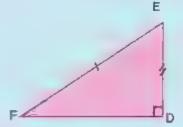


## Activity 4:

\* Draw any △ABC right-angled at B and △FDE, such that m (∠D) = m (∠B), FE = CA and ED = BC Measure AB, FD, ∠CAB, ∠EFD, ∠ACB and ∠FED

What do you notice?





- Vary △ABC and △DEF without changing the above conditions
   Move △DEF and check whether it falls exactly onto △ ABC.
   Is this sufficient so as △ ABC ≡ △ DEF?
- The forth case

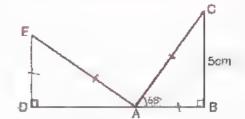
#### Right angle, Hypotenuse and side' test (RHS)

Two right- angled triangles are congruent if the hypotenuse and a side of one triangle are congruent to the Corresponding parts of the other triangle.

### Example

In the figure opposite,

Study the case of congruency then deduce: m (∠AED), length of AD



#### Solution:

 $\triangle$  ABC  $\equiv$   $\triangle$  EDA (RHS)

From the results of congruency then m ( $\angle AED$ ) = m ( $\angle CAB$ ) = 56°

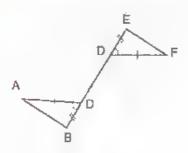
AD = CB = 5 cm

#### Dirll

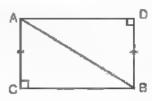
In the figures below the similar signs denote the congruency of the elements marked by these signs.

Mention the pairs of congruent and non congruent triangles (give reason).

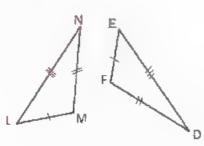
[1]



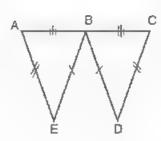
[5]



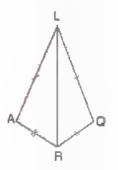
[2]



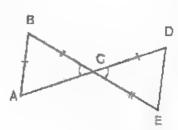
[6]



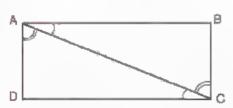
[3]



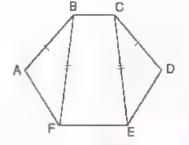
[7]



[4]



[8]



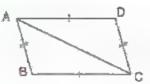
## Exercise (4-3)



The similar signs denote the congruency of the elements marked by these signs.

- Are the triangles congruent?
- Write a correct statement of congruence and state the test used

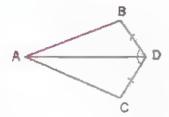
[a]



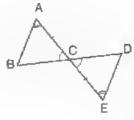
[e]



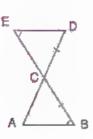
[b]



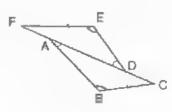
[f]



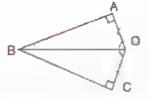
[0]



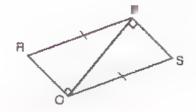
[g]

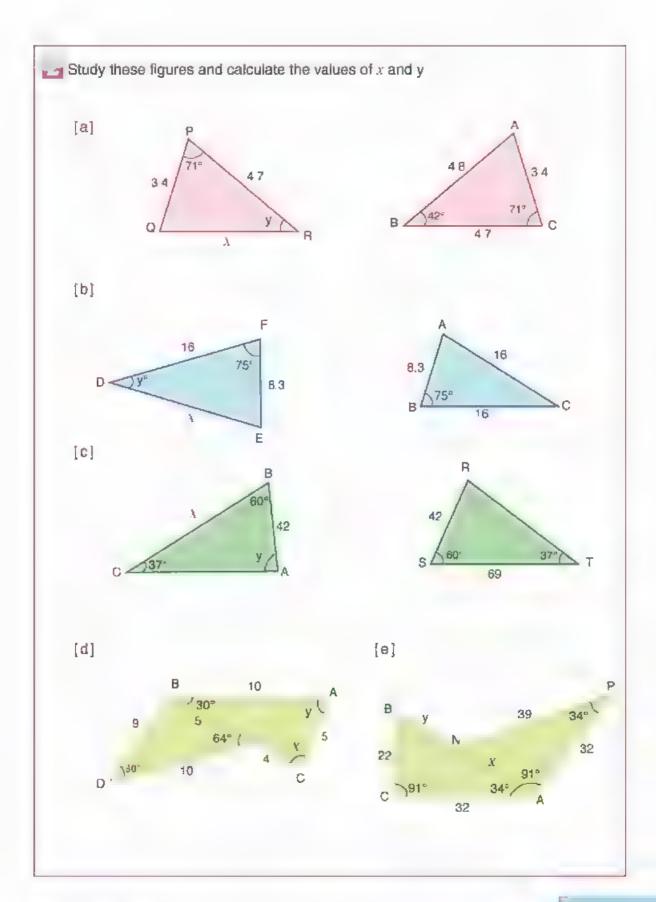


[d]

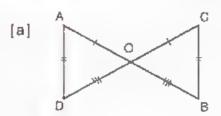


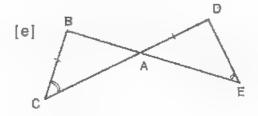
[h]

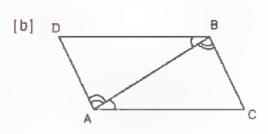


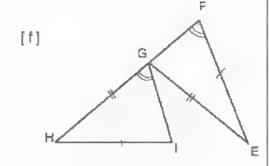


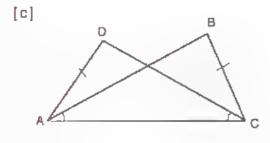
The similar signs denote the congruency of the elements marked by these signs. Find the two congruent triangles, give reasons and write down the results of congruence.

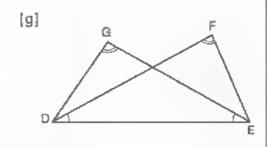


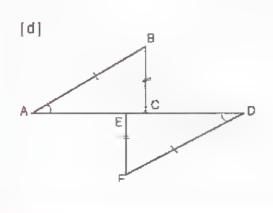


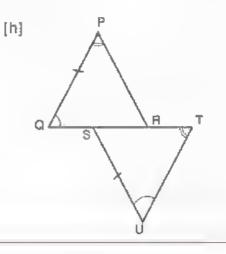












Study the data for  $\triangle$ ABC and  $\triangle$ XPG Are these triangles congruent? Write, if applicable, a correct statement of congruence and state the test used

[a] 
$$AB = PX$$
,  $AC = XG$ ,  $\angle A = \angle X$ 

[b] 
$$BC = PG$$
,  $BA = XP$ ,  $\angle B = \angle G$ 

$$[c]AB = PG, BC = PX, AC = XG$$

[d] 
$$AB = XP$$
,  $CA = GX$ ,  $\angle B = \angle P$ 

[e] 
$$\angle B \cong \angle G$$
,  $\angle C \cong \angle X$ ,  $BC = XG$ 

$$[f] \angle A = \angle X, \angle B = \angle P, AC = PG$$



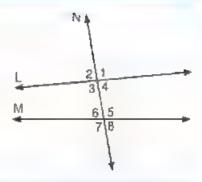
- [a] Two triangles are congruent if the lengths of sides of one triangle are equal to the corresponding parts of the other.
- (b) Two triangles are congruent if the measures of the angles of one triangle are equal to the measures of the corresponding parts of the other.
- [c] Two right- angled triangles are congruent if the lengths of two sides of one triangle are equal to the corresponding parts of the other triangle
- [d] Two right- angled triangles are congruent if the length of the hypotenuse and the measure of an angle differs from the right angle are equal to the corresponding parts of the other triangle.
- [e] Two right- angled triangles are congruent if the length of the hypotenuse and the length of a side of one triangle are equal to the corresponding parts of the other triangle.
- [a] Use a protractor to draw a triangle whose angles have measure 50°, 60°, and 70°
  - (b) Can you draw another triangle whose angles have measures 50°, 60°, and 70° but which is not congruent to the first triangle?

#### Lesson 4

## **Parallelism**

Draw two straight lines L and M, then draw a transversal N (a line that intersect them both).

Pairs of alternate, corresponding and interior angles are formed.

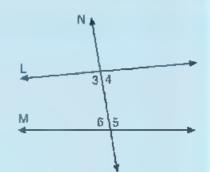


#### **Activities**

1 Complete:

∠ 3 and ∠ 5 are called alternate angles ∠ ..... and ∠ ...... are called alternate angles

In case of L is parallel to M, Notice the relation between the alternate angles.

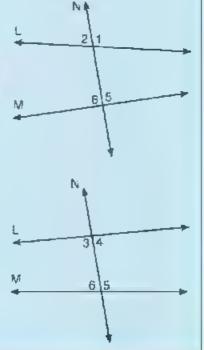


2 ∠ 1 and ∠ 5 are called corresponding angles.
∠... and ∠..., are called corresponding angles.

Determine two more pairs of corresponding angles

In case of L is parallel to M, notice the relation between the corresponding angles.

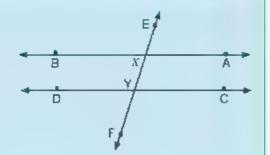
3 ∠ 4 and ∠ 5 are called interior angles on one side of the transversal, ∠ ..... and ∠ ..... are called interior angles on one side of the transversal In case of L is parallel to M, Notice the sum of two interior angles on one side of the transversal



Use your computer or geometrical instruments to carryout the following activities.

## Activity 1

From a point C which is not on AB, draw CD // AB, draw EF a transversal to intersect CD and AB at X and Y respectively, determine:

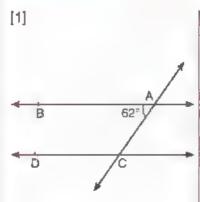


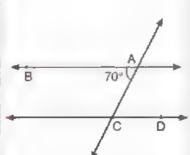
- The measures of two alternate angles.
- The measures of two corresponding angles.
- The measures of two interior angles on one side of the transversal, then add them vary the position of the transversal EF What do you notice?
- If a straight line intersects two parallel straight lines, then:
  - Every two alternate angles are equal in measure.
  - Every two corresponding angles are equal in measure.
  - Every two interior angles on one side of the transversal are supplementary.



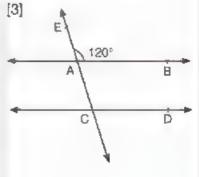
In each of the following figures, If AB // CD , then complete:

[2]





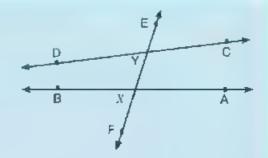
$$m (\angle ACD) = m (\angle ....)$$
  
= ....°



$$m (\angle ACD) = m (\angle ....)$$

## Activity 2

[a] Draw AB and CD, then draw the transversal EF to intersect them at X and Y respectively, determine:



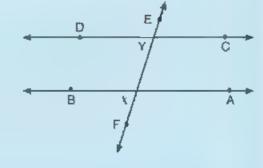
The measures of the two alternate angles

CYX and BXY

Rotate  $\overrightarrow{CD}$  about Y until m ( $\angle CYX$ ) = m ( $\angle BXY$ ). Test whether  $\overrightarrow{CD}$  is parallel to  $\overrightarrow{AB}$  by drawing  $\overrightarrow{MN}$  passes through Y and is parallel to  $\overrightarrow{AB}$ 

Determine once again the measure of the alternate angles CYX and BXY

- [b] Carryout similar activities as in [a] about:
  - [1] corresponding angles.
  - [2] interior angles on the same side of the transversal.



What do you notice?

- Two straight lines in a plane are parallel if they are cut by a transversal in such a way that:
  - The alternate angles are equal in measure.
  - The corresponding angles are equal in measure.
  - The interior angles on one side of the transversal are supplementary.

### Example

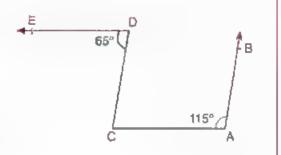
In the figure opposite,

Does AC // DE? why?

#### Solution:

$$m (\angle C) = 180^{\circ} - 115^{\circ} = 65^{\circ} \text{ because .....}$$

i e m (
$$\angle$$
C) = m ( $\angle$ D) = 65°



#### Drill

In the figure opposite,

m (
$$\angle$$
A) = 42°, and m ( $\angle$ C) = 117°

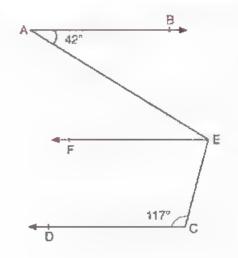
Determine m (∠AEC)

#### Solution:

$$m (\angle AEC) = m (\angle A) + m (\angle ....)$$
  
= ......  $^{o}$  + . . .  $^{\circ}$ 

= 0

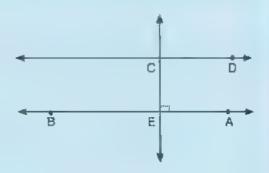
Because . ....



## Activity 3

Draw a straight line AB and mark a point C which is not on AB, draw CD // AB and a straight line through C perpendicular to AB intersecting AB at E. Measure ∠DCE.

Name the relationship between CD and CE vary the position of CE and CD.



What do you notice?

- A straight line that is perpendicular to one of two parallel lines is also perpendicular to the other.
- If each one of two straight lines is perpendicular to a third line in a plane, then the two straight lines are parallel.

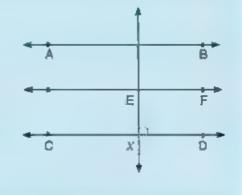
## Activity 4

Draw AB // CD , then draw EF // AB , then draw EX \_ CD and intersects it at X.

Measure ∠FEX

Is EF also parallel to CD ? Give your reasons Vary the position of Ex and CD.

What do you notice?



 If two straight lines are parallel to a third straight line, then these two straight lines are parallel to each other.

## Activity 5

Draw several parallel lines  $L_1$ ,  $L_2$ ,  $L_3$ ,  $L_4$  then draw the transversal  $M_1$  intersect them at A, B, C, and D respectively  $L_1 \leftarrow$  where AB = BC = CD. Draw the  $L_4 \leftarrow$  transversal  $M_2$  to intersect them at  $L_4 \leftarrow$  E, F, G, and H

Does EF = FG = GH?

What do you notice?

Vary the position of the transversal M<sub>2</sub>, what do you notice?

 If Parallel straight lines divide a straight line into segments of equal lengths, then they divide any other straight line into segments of equal lengths

#### Drill

In the figure opposite,

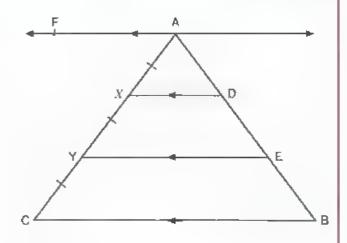
AX = XY = YC and AB = 12 cm

Find the length of BE

#### Solution:

Then AD = DE = EB

i.e BE = 
$$\frac{1}{3}$$
 AB = 4 cm



### Exercise (4-4):



#### Complete:

- [a] A straight line that is perpendicular to one of two parallel lines is also ...... to
- [b] A straight line that is parallel to one two parallel lines is also . . . to the other
- [c] When a transversal cuts two parallel lines.
  - [1] The alternate angles are .........
  - [2] THe corresponding angles are . ... ..
  - [3] The interior angles on the same side of the transversal are .......
- [d] Two straight lines in a plane are parallel if they are cut by a transversal in such a wayh that
  - [1] The ...... angles are equal, or
  - [2] The ..... angles are equal, or
  - [3] The ... angles on the same side of the transversal are supplementary.
- [e] If two straight lines intersect, then the measure of each two vertically opposite angles are ...
- [f] In this figure, if CD //  $\overline{BA}$  and  $\overline{DE}$  //  $\overline{CB}$ , then  $x = 1, ..., \infty$

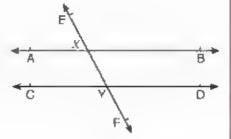




### in this figure:

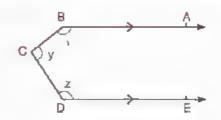
AB // CD . and EF is a transversal

- [a] What angles are equal in measure to ∠EXB? →
- [b] What angles are equal in measure to ∠XYC?



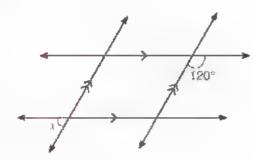
## 👪 In this figure.

 $\overrightarrow{BA}$  //  $\overrightarrow{DE}$  calculate: x + y + z. (Hint. Draw a line through C parallel to  $\overrightarrow{BA}$  ).

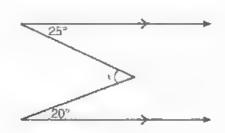


## Find the value of x in each figure:

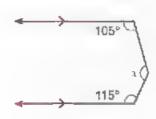
[a]



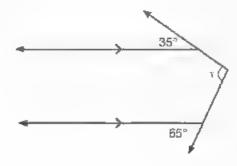
[d]



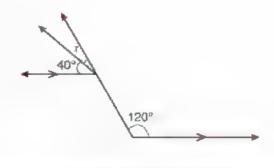
[b]



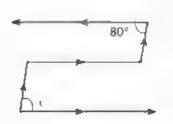
[e]



[c]



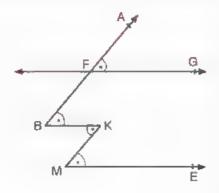
[f]



## 🔠 In this figure.

 $m (\angle AFG) = m (\angle B) = m (\angle K) = m (\angle M)$ write the four pairs of parallel lines.

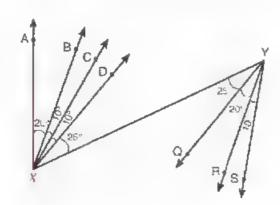
Give your reasons.



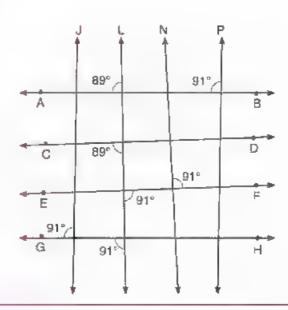
## in the these figures:

Name the pairs of parallel lines in each Figure:

[a]



[b]



#### Lesson 5

## **Geometric constructions**

## Constructing the bisector of a given angle

Given: ∠ABC is a given angle

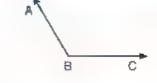
construction: The bisector of ∠ABC

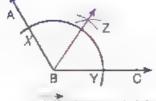
#### Procedure:

- With B as a centre and a sultable radius, draw an arc that intersects BA at X and BC at Y.
- With each of X and Y as centre and a suitable radius, draw two arcs which intersect at Z.
- Draw BZ



BZ is the .... of symmetry of ∠ABC.





BZ bisects ∠ ABC

## La Constructing a perpendicular from a point outside a straight line

Given: AB is a given straight line, P ∉ AB

Construction: The perpendicular to AB from P

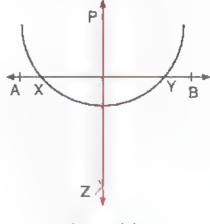
Procedure:

- With P as a centre and a suitable radius, draw an arc which intersects  $\overrightarrow{AB}$  at points X and Y.
- With each of X and Y as centres and a suitable radius, draw arcs which intersect at a point Z
- Draw PZ.

Complete:

PZ is the .... of symmetry of XY





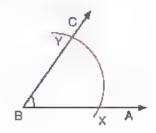
PZ 1 AB

## Constructing an angle to be congruent to a given angle:

Given: ∠ABC is a given angle

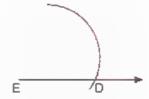
construction: drawing ∠DEF congruent to ∠ABC

"without using a protractor"

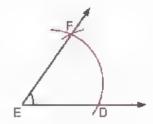


#### Procedure:

- Draw a ray with start point E to represent one of the sides of the required angle.
- Using the compasses, with B as a centre, and with suitable radius draw an arc to cut BA and BC at X and Y respectively and with E as a centre, and with the same radius, draw an arc to cut the ray at D.



- With X as a centre and with radius equals XY, then with D as a centre and with the same radius above, draw an arc to cut the first arc at F.
- Draw EF, then ∠DEF is congruent to ∠ . ......



Activity: Bisecting a line segment

Given: A B is defined line segment

Required: bisecting AB

#### Steps:

Draw the line segment AB.

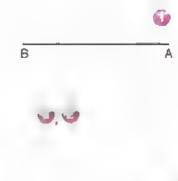
Place the sharp point of a compass at point

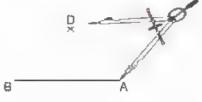
A, and adjust your compass to a length of

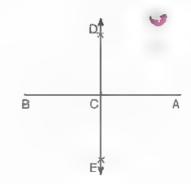
AB then draw 2 arcs at 2 different directions from AB.

Place the sharp point of the compass at point B, and with the same length, draw 2 arcs at the different directions of AB such that they intersect with the previous two arcs at points D, E

Draw DE to intersect AB at C, then, the point C becomes the midpoint of AB.







Drawing a perpendicular on a straight line that Passes by a point which belongs to that straight line.

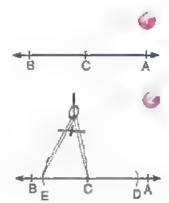
Given: AB is a defined straight line C ∈ AB

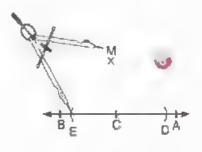
Required: Drawing a Perpendicular line on AB

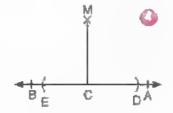
from point C

#### Steps:

- Draw AB and label AB
- Place the sharp point of a compass at C and adjust it to a suitable length then draw 2 arcs at 2 different directions from C Such that those arcs intersect AB at the two points D and E.
- Place the sharp point of a compass at both D and E and adjust it to a suitable length which is more than C D, then draw two arcs that intersect at point M.
- ₩C, then MC ⊥ AB







Drawing the scalene acute angled triante ABC, and draw an axis of symmetry for each side "don't erase the arcs" Do the axes of symmetry intersect in on point?.

#### Discuss:

If DEF is an obtuse angled triangle at E. Where do the axes of symmetry for its sides intersect?.

If XYZ is anight angled triangle at Y. Where do the axes of symmetry for its sides intersect?,

Measure the lengths of the line segments that connect the intersection point of the axes of symmetry with the vertices of the triangle in each case? What do you observe?

Two sharp point compass is used to measure the distance between two point

### 🌃 Activity:

Drawing a straight line from a given point parallel to a given straight line.

Given: AB is a given straight line, C ∉ AB

Required: Draw a straight line from point C parallel to A B

**▼**B A

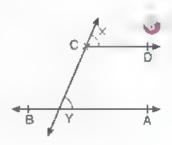
#### Steps:

Draw AB , C € AB

Draw XY crosses through the point C and intersects A B at Y.

At point C draw the angle XCD corresponding to ∠AYX such that ∠XCD = ∠XYA as shown in the previous activity.

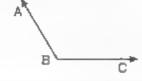
Then CD // AB



#### Exercise (4-5)

- Do the indicated construction (Don't remove the arcs)
  - [a] The perpendicular to AB from P
- [b] The bisector of ∠ ABC





[c] The bisector of Z XYZ



[d] The axis of symmetry of AB



- [a] Draw any acute angled triangle. Bisect each of the three angles.
  - [b] Draw any obtuse angled triangle. Bisect each of the three angles
  - [c] What do you notice about the points of intersection of the bisectors in parts (a) and (b)?
- [a] Draw any acute angle triangle construct the perpendicular bisector of each side
  - [b] Do the perpendicular bisectors intersect in one point?
  - [c] Repeat parts (a) and (b) using an obtuse angled triangle.
- [a] Draw any acute angled triangle. Construct the three altitudes.
  - [b] Do the straight lines that contain the altitudes intersect in one point?
  - [c] Repeat parts (a) and (b) using an obtuse angled triangles.
- Use the ruler and protractor to draw the traingle ABC in which AB = 5 cm, BC = 6 cm, and CA = 7 cm. D ∈ CB
  - [a] draw ∠DBE congruent to ∠A
  - [b] Complete:  $m(\angle ABE) = m(\angle .....)$

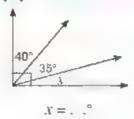
- Draw BC in a suitable length, using a compass and the unscaled ruler, bisect BC at D and from D draw the  $\overline{DA}$  perpendicular to  $\overline{BC}$ , then draw  $\overline{AB}$  and  $\overline{AC}$  Compare the lengths of  $\overline{AB}$  and  $\overline{AC}$  using the compass. What do you observe?.
- Draw the isosceles triangle ABC in which AB = AC using the compass, bisect  $\overrightarrow{BC}$  at D. Draw  $\overrightarrow{AD}$  and prove that  $\overrightarrow{AD} \perp \overrightarrow{BC}$ .
- Draw the right angled triangle XYZ at Y using compass and ruler only. Bisect XZ at M. Draw YM . Are MX = MY = MZ? Draw other right angled triangles and repeat the same construction, Are MX = MY = MZ?.

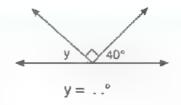
### **UNIT TEST**

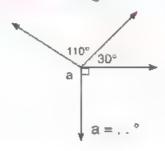
Answer all the questions

#### Complete:

[a] Calculate the measure of the unknown angle in each of the following:







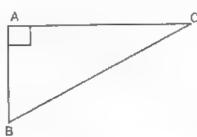
[b] For each of the following angles, write the closest measure from the following: 80°, 120°, 240°.







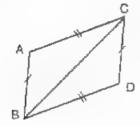
[c] Write the line segment which represents the hypotenuse in the triangle .......



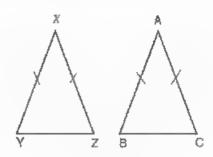
- [a] Using a ruler and the compass, draw a triangle ABC in which AB = AC = 7 cm, BC = 6 cm. Bisect  $\angle B$  and  $\angle C$  by two bisectors which intersect at M. Is MB = MC?
  - [b] Using a ruler and a compasses, draw the triangle ABC in which AB = AC = 5 cm, BC= 6 cm, then draw AD  $\perp$  BC Where AD  $\cap$  BC = {D} Measure the length of AD. (Don't remove the arcs).
- Using the ruler and the compasses draw A ABC and bisect each of AB, AC at D,E respectively. Draw DE.
  - [a] Using the compasses, measure DE and satisfies that BC = 2DE
  - [b] is ∠ABC = ∠ADE? Does DE // BC?.

- Draw  $\triangle$  ABC in which AB = 4 cm, BC = 5cm and AC = 6cm. Construct the perpendicular bisectors of Triangle sides. What do you notice?.
- In the following figures, Find the two congruent triangles, give reasons, and write down the results of congruence.

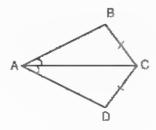
[a]



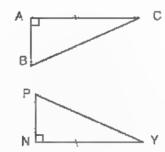
[d]



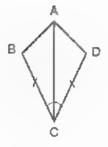
[b]



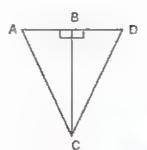
[e]



[c]

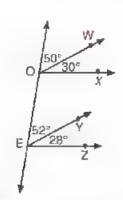


[f]

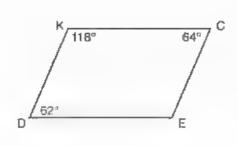


State which segments are parallel in each figure?

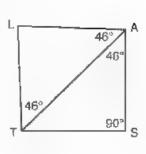
[a]



[b]



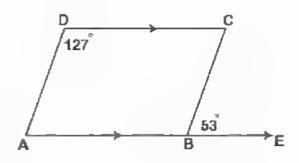
[c]



In the figure opposite:

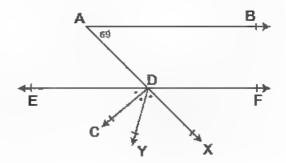
$$m (\angle 1) = m (\angle 4)$$
,  
 $\overrightarrow{BC} / \overrightarrow{FD}$   
Does  $\overrightarrow{BA} / \overrightarrow{DF}$ ?  
give reason

👪 In the opposite figure:



In the opposite figure:

$$\overrightarrow{AB} \# \overrightarrow{FE}, \overrightarrow{EF} \cup \overrightarrow{AX} = \{D\}$$
 $m (\angle DAB) = 69^{\circ}$ 
 $m (\angle XDY) = m (\angle YDC)$ 
 $= m (\angle CDE), \text{ find}$ 
 $m (\angle CDE)$ 



### Models of Examinations of Algebra and Statistics

### Model (1)

#### Answer the following questions:

#### Q1) Complete each of the following:

- 1)  $2\frac{1}{5} \times \dots = 1$
- 3) 0.18 30% = ....
- 4)  $7 x^3 y^2 x \dots = 21 x^3 y^5$
- 5)  $(2 \times -3) (x + 5) = 2x^2 + \dots -15$

#### Q21 Choose the correct answer from those given :

- 1) The rational number that lies on third of the way between 8 and 12 from the smaller is  $\frac{1}{3}$ , 10,  $9\frac{1}{3}$ , 10,  $\frac{2}{3}$ ]
- 2) If the mode of the values 7, 5, x + 4, 5, 7 is 5 than x = ...... [1, 4, 5, 7]
- 3) If  $\triangle + \Box = 20$ ,  $\triangle + \triangle + \Box = 35$  then  $\triangle = ............. [15, 20, 5, 10]$
- 4) The arithmetic mean of the set of values 1 , 6 , 4 , 8 , 6 is ...... [25 , 5 , 6 , 8]
- 6)  $0.7 \pm 0.3 = \dots$  [1, 3.7, 0.37,  $1\frac{1}{30}$ ]

#### Q3), a) subtract:

- a)  $5x^2 + y^2 3xy + 1$  from  $6x^2 2xy + 3y^2$
- b) Use the distribution property find the value  $\frac{27}{16} \times \frac{11}{7} \div \frac{27}{16} \times \frac{11}{7} \frac{27}{16} \times \frac{6}{7}$  ( without using the calculator )

- a) Simplify to the simplest from :  $(2 \times -3)(2 \times +3) + 7$ , and calculate the numerical value of the result when x = -1
  - b) Find three rational numbers that lie between  $\frac{1}{2}$ ,  $\frac{1}{3}$
- **Q5).** a) Divide:  $2x^3 + 3x^2 4x 6$  by 2x + 3
  - b) The following table shows Gehad's mark of mathematics in 6 months:

Month	October	November	December	February	March	April
Marks	30	35	42	37	44	50

Find the arithmetic mean of the marks.

#### Q1) Complete each of the following:

1) 
$$24 x^4 y^6 = 6x^2 y^3 \times ...$$

5) 
$$5x^2 + 15xy = 5x (... + ... + ...$$

#### Q2), Choose the correct answer from those given:

4.5	The state of the s	- 3.2		-1	
11	The algebraic term	1 6x"V"	is of	degree	è

- a) third b) fourth c) fifth
- d) sixth

2) The retional number that lies in half way between 
$$\frac{1}{3}$$
 and  $\frac{5}{9}$  is . .

- b) 3

- 3) He multiplicative inverse of the member  $\left(\frac{1}{2}\right)^{z=0}$  is ... .........
  - a) 2
- b) -2
- c) 1
- d) -1

4) If 
$$\frac{5}{x+2}$$
 is a rational number, then  $x \neq \dots$ 

- a) -2
- b) zero
- c) 2
- d) 5

- a) 4
- b) 5 c) 7
- d) 16
- IF the arithmetic mean for the set of values 3, 5, x + 2 is 4, then the arithemetic mean for the two values 5-X ,5 + 2 X is ....

(6.4.3.2)

- (03) a) Use the distribution property. Find the value of :  $\frac{3}{7} \times 2 + \frac{3}{7} \times 6 = \frac{3}{7}$ 
  - b) Find three rational numbers that lie between  $\frac{1}{2}$  ,  $\frac{1}{3}$  .
- Q4) a) What is increase of 7x + 5y + z than 2x + 6y + z.
  - b) Divide:  $14x^2y 35xy^2 + 7xy$  by 7xy,  $x \neq zero$ ,  $y \neq zero$ .
- a) Simplify to simplest from: (x 3) (x + 3) + 9 and calculate the numerical value of the result when x = 5.
  - b) If the arithmetic mean of the numbers 8, 7, 5, 9, 4, 3, k + 4 is 6, then find the value of k.

# Model (3)

### Merge Studants

#### Q1) Complete each of the following:

- 1) The algebraic term 5 x y is of ...... degree.
- 2)  $(x-3)(\dots + \dots) = x^2 9$
- The rational number which hasn't multiplicative inverse is ....
- 5) The number  $\frac{4}{x}$  is a rational number if  $x \neq \dots$

#### Q2) Choose the correct answer from those given:

- 2) The arithmetic mean of the set of values 2, 3, 8, 2, 5 = .............[3, 2, 4, 8]
- 3) The additive inverse of the number -3 is . . . . . . . . . . . . . . . . [-3, 3,  $\frac{1}{3}$ ,  $-\frac{1}{3}$ ]
- 4) The remainder of subtracting 7 x from 9 x = ... ... [2x, 16 x, -2 x, zero]
- Q3) a) Use the distribution property. Complete to find  $\frac{5}{7} \times 8 + \frac{5}{7} \times 5 + \frac{5}{7}$

= 
$$\frac{5}{7}$$
 (....+...)

### Q4) Put true ( 1 ) or false (x)

1) The quotient of  $12x^4 + 6x$  by 6x is  $2x^3 + 1$ 

2) The H.C.F of  $15x^{6} + 5x$  is  $5x^{6}$ 

3) The rational number that lies between  $\frac{1}{4}$  and  $\frac{3}{4}$  is  $\frac{1}{2}$ 

4) 5x + 3x = 8x ( )

5)  $(x + 4)^2 = x^2 + k + 16$  then k = 4x

### Q5) Match from column (A) to column (B):

(A)			(B)	
1) If $\frac{x-7}{5}$ = zero, then $x = \dots$	*	t	3	
2) $3x^2 + 15y = (x^2 + 5y)$	jk.	*	7	
3) $(3x + 5) + (4x - 5) = \dots$	99	*	50	
4) 1/2 = %	4	:lk	1	
5) If $\frac{A}{B} = \frac{1}{2}$ , then $\frac{2A}{B} = \dots$	sk	all .	7x	

### **Models of Examinations of geometry**

### Model (1)

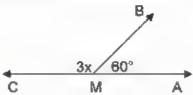
#### Q1) Complete each of the following:

- 2) In the opposite figure: if  $\triangle$  ABC =  $\triangle$  XYZ, m ( $\angle$  A) + m ( $\angle$  B) = 140°, then m ( $\angle$  Z) = ......° A





- 3) If m ( $\angle$  B) = 105°, then m (reflex  $\angle$  B) = ............°



5) The two right - angled triangles are congruent if ...........

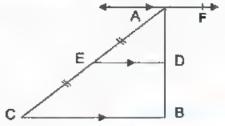
#### Q2) Choose the correct answer from those given:

1) If  $\angle$  x =  $\angle$  y ,  $\angle$  , x ,  $\angle$  y are supplementary angles, then m ( $\angle$  x) = ... ...°

[45,90,135,180]

2) In the opposite figure : AF / DE / CB , AE = EC then AD : AB = ... . .... : .......

[2:1 , 3:2 , 1:3 , 1:2]



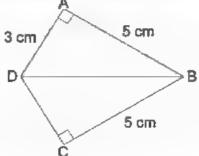
- 3) The two straight lines that are perpendicular to a third, then the two straight lines are

  [perpendicular, intersecting, congruent, parallel]
- 4) The measure of each of the two equal complementary angles equals .... ...°

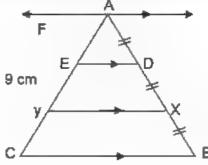
  [180 , 45 , 360 , 90]
- 5) If two straight lines intersect, then each two = ...... angles have the same measure.
  [vertically opposite, adjacent, alternate, corresponding]
- 6) If  $\triangle$  ABC  $\equiv$   $\triangle$  LMN, then m ( $\angle$  ACB) = m ( $\angle$ ......)

[LMN, MLN, LNM, NLM]

23) a) In the opposite figure: m ( $\angle$  BAD) = m ( $\angle$  BCD) = 90°, AB = CB = 5cm, AD = 3 cm, mention the conditions for  $\triangle$  ABD,  $\triangle$  CBD to be congruent and find the length of  $\overline{CD}$ ,

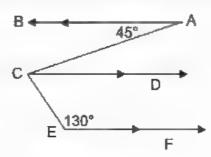


b) In the opposite figure:  $\overrightarrow{AF} /\!\!/ \overrightarrow{DE} /\!\!/ \overrightarrow{XY} /\!\!/ \overrightarrow{BC}$ ,  $\overrightarrow{AD} = \overrightarrow{DX} = \overrightarrow{XB}$ ,  $\overrightarrow{AC} = 9$  cm. Find the length of  $\overrightarrow{AY}$ , given the reason.

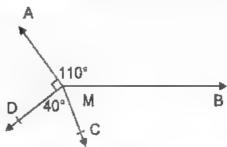


a) In the opposite figure:  $\overline{AB}/\overline{CD}/\overline{EF}$ , m ( $\angle$  A) 45°, m ( $\angle$  E) = 130°,

find m (∠ ACE)

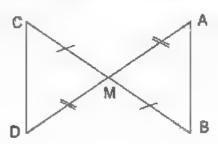


b) In the opposite figure:  $m (\angle AMB) = 110^{\circ}$ ,  $m (\angle AMD) = 90^{\circ}$ ,  $m (\angle DMC) = 40^{\circ}$ . Find with steps  $m (\angle BMC)$ .



a) In the opposite figure:  $\overline{AD} \cap \overline{BC} = \{M\}$ , BM = MC, AM = MD, write the conditions

for △ AMB = △ DMC to be congruent.



b) By using your geometric instruments draw ∠ ABC whose measure 110°. Draw BF to bisect the angle.



#### Q1) Complete each of the following:

- 1) The sum of the measures of the accumulative angles at a point = ..... "

- 4) The two right-angled triangles are congruent if
- 5) The two adjacent angles formed by intersecting a straight line and a ray are

#### Q2) Choose the correct answer from those given:

- 1) If  $\angle$  x complements  $\angle$  y,  $\angle$  x  $\in$   $\angle$  y, then m ( $\angle$  x) = ...... [45°, 90°, 180°, 360°]
- 2) The number of triangles in the opposite figure equals . . . . . . . . [4, 6, 7, 8]



- 4) △ ABC = △ XYZ, m (∠ A) + m (∠ B) = 100°, then m (∠ Z) = ......°

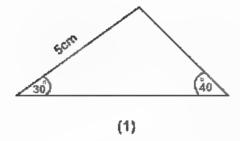
[50,80,90,100]

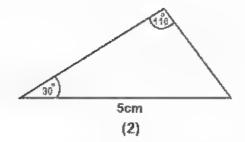
5) The two straight lines that are perpendicular to a third, then the two straight lines are . . . . . . . [perpendicular , parallel , congruent , intersecting]

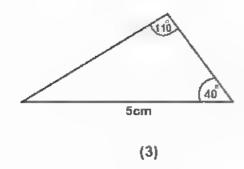
6) The Figure number ...... does not (1,2,3,4)

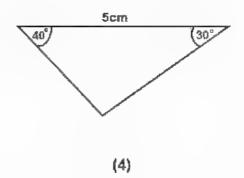
#### Congruent with the opposite figure



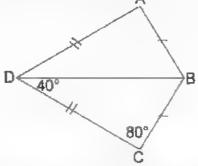




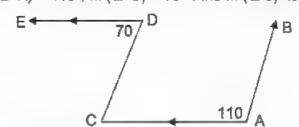




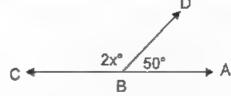
- (Q3) a) mention two cases of congruency of two triangles.
  - b) In the opposite figure AB = BC, AD = CD, m ( $\angle$  C) = 80°, m ( $\angle$ BDC = 40° Prove that  $\triangle$  CBD  $\cong$   $\triangle$  ABD and find m ( $\angle$  ABD)



a) In the opposite figure  $\overline{DE}/\!\!/\overline{AC}$ , m ( $\angle$  A) = 110°, m ( $\angle$  D) = 70° Find m ( $\angle$  C) is  $AB/\!\!/\overline{CD}$ ? Given the reason.  $E \blacktriangleleft 70/\!\!/D$ 



- b) By using the ruler and the compasses draw the angle ABC where  $m~(\angle~B)=80^{\circ} and~draw~B\vec{D}~~to~bisect~the~angle~~Don't~remove~the~arcs).$
- Q5) a) In the opposite figure AC ∩ BD = {B} m (∠ ABD) = 50°, m (∠ DBC) = 2x°, find in degrees the value of x.



b) In the opposite figure  $\overrightarrow{BD}$  bisects  $\angle$  ABC , m ( $\angle$  DBC) = 35°, m ( $\angle$  BDC) = 120°. Find m ( $\angle$  A) with degrees.

## Model (3)

Merge Studants

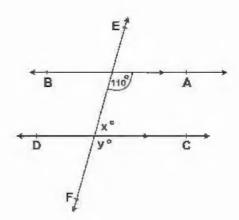
### Q1) Complete each of the following:

1)	If m ( $\angle$ A) = 100°, then m (reflex $\angle$ A) =°	
2)	The angle whose measure 50° complements an angle of measure°	
3)	The two straight lines parallel to a third are	
4)	The two triangles are congruent if two sides and are congruent.	
5)	If $\triangle$ ABC $\equiv$ $\triangle$ XYZ, then m ( $\angle$ Z) = m ( $\angle$ )	
2) C	hoose the correct answer from these given:	
1)	The sum of the measures of the accumulative angles at a point°	
	[630°, 180°, 90°, 360°]	
2)	The axis of symmetry of a line segments is	
	[perpendicular form its midpoint, parallel to it, equal to it, congruent to it]	
3)	The supplement of the angle whose measure is 30°=	
	[ 60°, 180°, 150°, 90°]	
4)	The angle whose measure is more than 90° and less than 180° is angle	
	[ obtuse , acute , right , straight]	
5)	If $\triangle$ ABC $\equiv$ $\triangle$ XYZ, then AB $\Rightarrow$ [XY , XZ , YZ , BC]	
33	Put ( ) for the correct statement and ( X ) for the in correct statement	
1)	The right - angled triangle congruent with the equilateral triangle (	
2)	The two angles whose measures 100°, 80° are supplementary (	•

### 3) In the opposite figure:

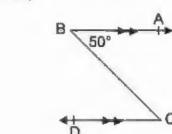
**b)** 
$$X = 70^{\circ}$$
 ( )

c) 
$$y = 180^{\circ}$$
 (



#### Q4) a) in the opposite figure:

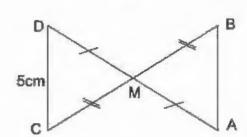
Then, 
$$m (\angle ABC) = m (\angle \dots)$$



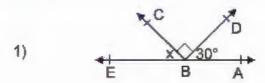
#### b) In the opposite figure complete:

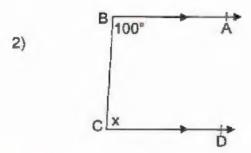
1) 
$$\triangle$$
 ABM  $\equiv$   $\triangle$  .........

3) m (
$$\angle$$
 B) = m ( $\angle$  ......)

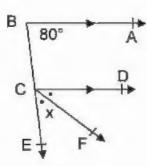


#### Q5) In the all figures opposite find the value of x:



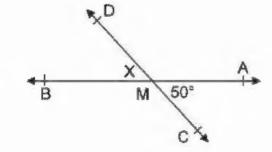


3)



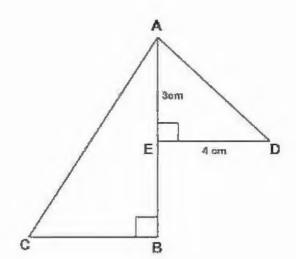
X = ......

4)



5) In the opposite figure:

If 
$$\triangle$$
 ABC  $\equiv$   $\triangle$  DEA



#### الرياضيات ص ١ ع انجليزي ف١

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